

Developments in Double-Modulated Terahertz Differential Time-Domain Spectroscopy

by

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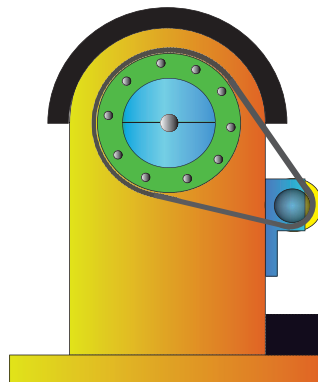
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Modelling terahertz signal extraction using lock-in amplifier

MODELLING terahertz signal extraction using a lock-in amplifier device is explained in this chapter. The first part of the chapter gives a detailed explanation on conventional THz-TDS signal extraction using a single lock-in amplifier. The second part discusses details of double-modulated THz-DTDS signal extraction using two lock-in amplifiers. Mathematical expression and matlab simulation are included to elaborate the signal extraction techniques further for both conventional THz-TDS and double-modulated THz-DTDS.

The double-modulated THz-DTDS modelling technique described in this chapter is also used in Ch. 7 to model the rapid succession measurement using the spinning wheel.

A.1 Terahertz signal recovery using lock-in amplifier

Recovering a very small signal in the presence of much larger background noise signal can be challenging. For example, in a T-ray spectrometer, an electro-optical or a photoconductive switching technique is employed where it often requires detection of small signals in the presence of a large noise signal. An illustration of a small signal hidden in a large noisy signal is shown in Fig. A.1. Typically, the large noise signal is composed of white noise and $1/f$ noise. It has been shown that the white noise can be reduced by simply averaging the output signals with respect to time, however this principle may not be applicable to the $1/f$ noise (Libbrecht *et al.* 2003). According to Libbrecht *et al.* (2003), the $1/f$ noise often originates from slow drifting of amplifiers and other noise generating elements over time. It has also been reported that the $1/f$ noise commonly present at very low frequencies (Dutta and Horn 1981). There are a number of ways to reduce the effect of $1/f$ noise. Conventionally, modulating the signal of interest using a mechanical chopper and recovering it using a tuned amplifier have been used widely (PerkinElmer-Instruments 2000). However, this technique is limited by the selectivity, Q factor, which may result in measurements of noise components due to a large bandwidth selection (PerkinElmer-Instruments 2000). Another approach is by using a lock-in amplifier. The lock-in amplifier allows *synchronous demodulation* or *phase sensitive detection* (PSD). The synchronous demodulation or PSD refers to a measurement of signal of interest that is synchronised in phase and frequency with the incoming reference signal. Furthermore, the lock-in amplifier is capable of providing narrowband filtering which allows an accurate measurement of the signal of interest with minimal noise interference (Stanford-Research-Systems 1999).

Traditionally, the terahertz signal generated from the conventional THz-TDS spectrometer and the double-modulated THz-DTDS spectrometer is recovered by using the lock-in amplifier. The noise present in these spectrometers is limited to not only white noise and $1/f$ noise but also other noise such as T-ray noise and laser fluctuations. In this chapter, modelling of terahertz signal extraction for a conventional THz-TDS spectrometer and a double-modulated THz-DTDS spectrometer are presented. For simplicity of the modelling, only white noise and $1/f$ noise originating from slow drifting amplifiers have been considered in this work.

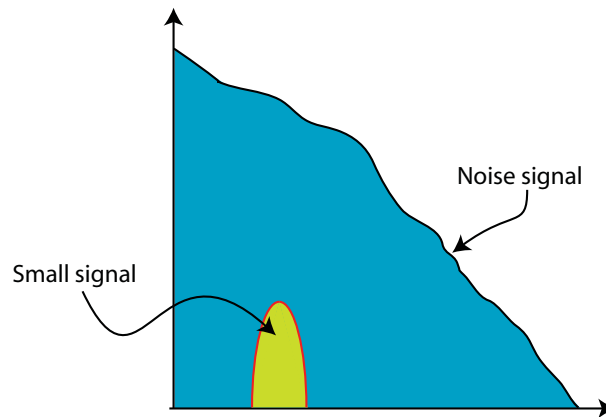


Figure A.1. Small signal hidden under a large noise signal. This figure illustrates the signal of interest hidden under a large noise signal. The noise signal is commonly originate from the white noise and the $1/f$ noise.

A.1.1 Objectives and framework

This chapter is focused on modelling the terahertz signal extraction from lock-in amplifier for terahertz time-domain spectroscopy (THz-TDS) and a double-modulated terahertz differential time-domain spectroscopy (double-modulated THz-DTDS). The modelled terahertz signal is added with white noise and $1/f$ noise for demonstration purposes. This chapter is structured as follows: In Sec. A.2, the lock-in amplifier configuration for terahertz signal extraction from a standard THz-TDS is described. In this section, a detailed description on the mathematical expression for terahertz signal recovery is given. Furthermore, a Matlab simulation for further elaboration of the concept is discussed. A lock-in amplifier configuration for double-modulated THz-DTDS is described in Sec. A.3. A detailed mathematical expression and simulation results to further elaborate the terahertz signal recovery are also discussed in this section followed by the chapter summary in Sec. A.4.

A.2 Terahertz signal extraction for a THz-TDS

In this section, modelling of the terahertz signal extraction for a conventional THz-TDS spectrometer using single lock-in amplifier is discussed. Figure A.2 shows a block diagram of a lock-in amplifier used for capturing terahertz signal. The incoming time delay dependant terahertz signal is denoted as $E(\tau_n)$ and the chopper input reference signal as $E_c(t)$.

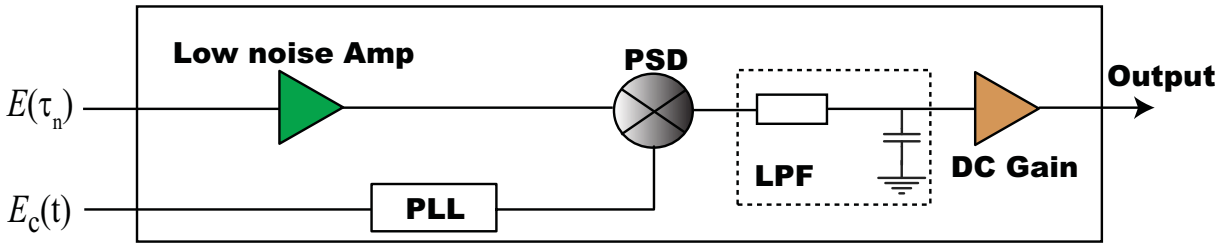


Figure A.2. Lock-in amplifier setup for conventional THz-TDS small signal recovery. This figure illustrates a block diagram of a lock-in amplifier. In a nutshell, the lock-in amplifier operates as multiplier with a narrowband filtering function.

A.2.1 Mathematical expression of the THz-TDS signal recovery using a single lock-in amplifier

Assuming that the chopper modulated terahertz signal, $E(\tau_n)$ is a square wave signal with an averaged amplitude, A_{τ_n} varying with the time delay, τ_n ,

$$E(\tau_n) = A_{\tau_n} \left(\frac{4}{\pi} \sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_{\text{chopper}}t + \phi_{\text{chopper}})}{(2k-1)} \right). \quad (\text{A.1})$$

Here, n is the step number determined by the delay stage. The $\omega_{\text{chopper}} = 2\pi f_{\text{chopper}}$ represents the modulating chopper frequency. Also, the ϕ_{chopper} refers to the chopper phase. This signal is amplified at the input of the lock-in amplifier with an AC gain of G_{ac} . Thus, the amplified signal can be written as follows:

$$E_{\text{ac}}(\tau_n) = G_{\text{ac}} E_{\tau_n}. \quad (\text{A.2})$$

The external chopper reference signal is obtained from a function generator that is used for modulating the optical beam. This signal is used as a reference input signal in the lock-in amplifier for signal demodulation. The external chopper reference signal can be written as follows:

$$E_c(t) = V_f \frac{4}{\pi} \left(\sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_c t + \phi_c)}{(2k-1)} \right), \quad (\text{A.3})$$

where $\omega_c = 2\pi f_c$ is the reference frequency with phase, ϕ_c . Here, the chopper reference signal is phase-locked loop for synchronising the frequency and phase components

with respect to the incoming terahertz signal before reaching the phase sensitive detector (PSD). The PSD act as a multiplier to produce an output signal that is a product of $E_{ac}(\tau_n)$ and $E_c(t)$,

$$E_{psd}(\tau_n) = E_{ac}(\tau_n)E_c(t) , \quad (A.4)$$

which can be also written as follows:

$$E_{psd}(\tau_n) = G_{ac}A_{\tau_n}V_f \frac{4}{\pi} \left(\sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_{chopper}t + \phi_{chopper})}{(2k-1)} \right) \frac{4}{\pi} \left(\sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_c t + \phi_c)}{(2k-1)} \right) . \quad (A.5)$$

Assuming that the chopper phase, $\phi_{chopper}$, is synchronised to ϕ_c and the chopper frequency, $\omega_{chopper}$ is synchronised to ω_c , the modulated signal at every time delay, τ_n is frequency-shifted after the demodulation stage. The demodulated output is then low-pass filtered to remove the double frequency components and keep the DC component. Since the lock-in amplifier considers only the first harmonic, one may write the demodulated output as follows:

$$E_{psd}(\tau_n) = \frac{1}{2}G_{ac}A_{\tau_n}V_f[1 - \cos(2\omega_{chopper}t)] . \quad (A.6)$$

Thus, the output signal after filtering can be written as:

$$E_f(\tau_n) = \frac{1}{2}G_{ac}A_{\tau_n}V_f . \quad (A.7)$$

After the filtering process, the DC output can be further amplified by introducing a DC gain, G_{dc} . Thus, the time delay dependant amplified signal at the output channel of the lock-in amplifier is

$$E_{dc}(\tau_n) = \frac{1}{2}G_{ac}G_{dc}A_{\tau_n}V_f . \quad (A.8)$$

Figure A.3 shows a simulation results of terahertz signal extraction for a standard THz-TDS. This figure is captured at a time delay of τ_n .

Therefore, the sum of all dc components obtained at timing delay, τ_1 till τ_n produces a temporal THz pulse. This process may take several minutes depending on time constant setting of the lock-in amplifier.

A.3 Terahertz signal extraction for a double-modulated THz-DTDS

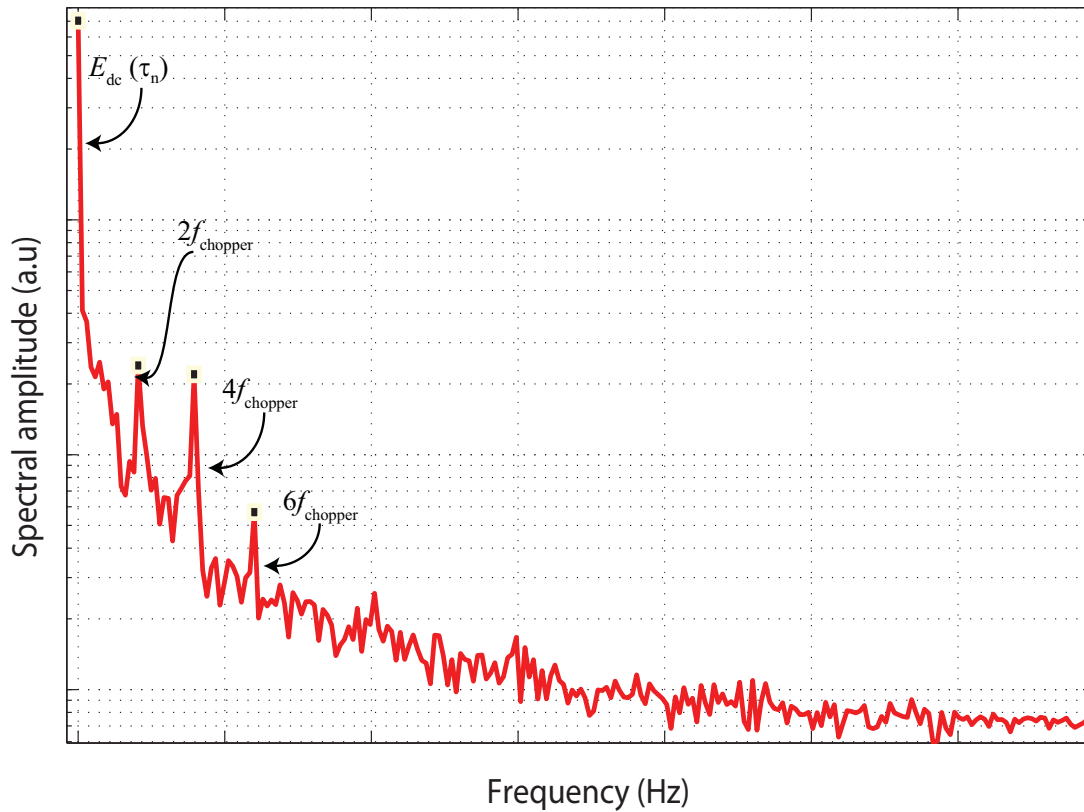


Figure A.3. Simulated terahertz signal extraction for a standard THz-TDS at the n th step of the delay stage. This figure shows the FFT of the signal detected after the demodulation and filtering stages of the lock-in amplifier. For demonstration purposes, the optical beam for generation of terahertz signal is set at f_{chopper} . The DC component, E_{dc} shown in the figure can be extracted by selecting a longer time constant. Longer time constant will result in narrower bandwidth, which means that the $2f_{\text{chopper}}$ component and above will be eliminated and only the dc component at n th step, $E_{\text{dc}}(\tau_n)$ is detected at the output channel of the lock-in amplifier.

A.3 Terahertz signal extraction for a double-modulated THz-DTDS

In the previous section, modelling of the terahertz signal using single lock-in amplifier has been discussed. By using the basic knowledge obtained from the above model, terahertz signal extraction for the double-modulated THz-DTDS is described in this section. Figure A.4 shows a block diagram of the lock-in amplifier configuration used for capturing terahertz signal from the double-modulated THz-DTDS spectrometer.

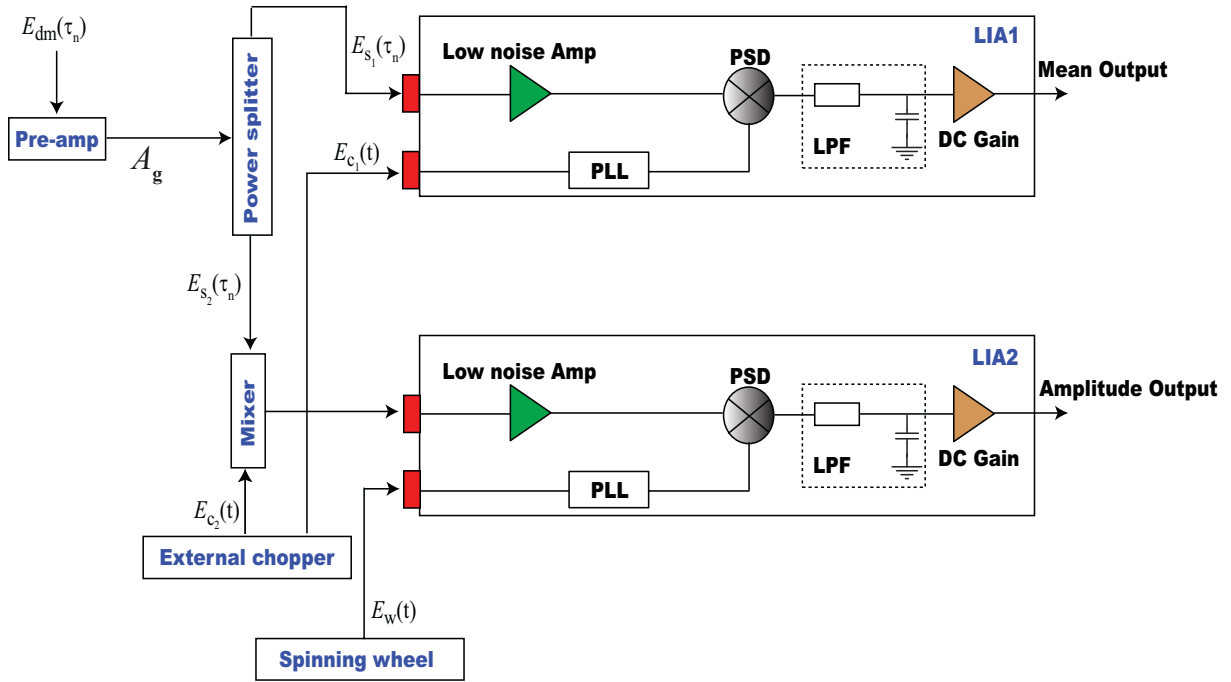


Figure A.4. Lock-in amplifier setup for double-modulated THz-DTDS small signal recovery.

This figure illustrates a block diagram of dual lock-in amplifier configuration used in the double-modulated THz-DTDS spectrometer.

A.3.1 Mathematical expression of the double-modulated THz-DTDS signal recovery using two lock-in amplifiers

Assuming that the double-modulated terahertz signal, $E_{dm}(\tau_n)$ is a square wave like signal, one may write the double-modulated terahertz signal as follows:

$$E_{dm}(\tau_n) = A_{\tau_n} \left(\left(1 + \frac{4}{\pi} \sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_{chopper}t + \phi_{chopper})}{(2k-1)} \right) \times \left(\frac{x-d}{x} \left(1 + \frac{4}{\pi} \sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_{wheel}t + \phi_{wheel})}{(2k-1)} \right) + d \right) \right), \quad (\text{A.9})$$

where A_{τ_n} is the averaged amplitude with varying time delay, τ_n and n is the step number determined by the delay stage. Here, x is the thickness of the reference sample. The sample material thickness is defined as d . Here, the $\omega_{chopper} = 2\pi f_{chopper}$ and $\omega_{wheel} = 2\pi f_{wheel}$ represent the chopper frequency and the spinning wheel frequency respectively. Also, $\phi_{chopper}$ refers to the chopper phase and ϕ_{wheel} refers to wheel phase. The detected double-modulated signal is further amplified using a low-noise pre-amplifier

A.3 Terahertz signal extraction for a double-modulated THz-DTDS

before entering the 2-way power splitter. The time delay dependant amplified signal, $E_p(\tau_n)$ can be written as follows:

$$E_p(\tau_n) = A_g E_{dm}(\tau_n), \quad (\text{A.10})$$

where A_g denotes the gain applied to the detected signal. The amplified signal is then split using a 2-way power splitter to produce the split signals, $E_{s_1}(\tau_n)$ and $E_{s_2}(\tau_n)$. These signals enter the input channel of the lock-in amplifier one (LIA1) and the input channel, $X_{\text{modulator}}$ of the mixer respectively. The $E_{s_1}(\tau_n)$ and $E_{s_2}(\tau_n)$ are described as follows:

$$E_{s_1}(\tau_n) = E_{s_2}(\tau_n) = \frac{1}{2} E_p(\tau_n). \quad (\text{A.11})$$

An AC gain applied at the input of the LIA1:

$$E_{ac_1}(\tau_n) = G_{ac_1} E_{s_1}(\tau_n). \quad (\text{A.12})$$

According to the lock-in amplifier configuration shown in Fig. A.4, an external chopper reference frequency is required for demodulation process at the LIA1 and the mixer. The chopper reference frequency is generally obtained from the frequency generator used for modulating the optical beam path discussed in Ch. 3. In this configuration, a splitter is used to split the incoming chopper frequency before entering the input reference channel of the LIA1 and the X_{carrier} input reference channel of the mixer. The external reference signal can be written as follows:

$$E_{c_1}(t) = E_{c_2}(t) = \frac{1}{2} \left(1 + V_c \frac{4}{\pi} \left(\sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_c t + \phi_c)}{(2k-1)} \right) \right), \quad (\text{A.13})$$

Here, $\omega_c = 2\pi f_c$ is the reference frequency with phase, ϕ_c . The phase sensitive detector (PSD) of LIA1 produces an output signal that is a product of $E_{ac_1}(\tau_n)$ and $E_{c_1}(t)$. This stage is also known as demodulation stage. Hence, the PSD output of LIA1 is

$$E_{psd_1}(\tau_n) = E_{ac_1}(\tau_n) E_{c_1}(t). \quad (\text{A.14})$$

Assuming that the chopper phase, ϕ_{chopper} , is synchronised to ϕ_c and the chopper frequency, ω_{chopper} is synchronised to ω_c , the double-modulated signal is frequency-shifted after the demodulation stage. The demodulated output is then low-pass filtered to remove the redundant information and only DC component will be taken into account for DC amplification. Thus, the output signal detected at LIA1 is denoted as the time delay dependant mean signal, $E_{\text{mean}}(\tau_n)$.

On the other hand, the $E_{s_2}(\tau_n)$ entering the $X_{\text{modulator}}$ input channel of the mixer is multiplied with the $E_{c_2}(t)$. The mixer is designed without filtering effect so that better accuracy on the signal extraction at the LIA2 can be obtained as compared to the previously presented works (Mickan *et al.* 2002b, Mickan *et al.* 2004, Balakrishnan *et al.* 2006, Balakrishnan *et al.* 2008). The product of the mixer is then fed into the input channel of the LIA2. The product of the mixer can be written as follows:

$$P_{\text{out}}(\tau_n) = kE_{s_2}(\tau_n)E_{c_2}(t), \quad (\text{A.15})$$

where k is the scaling factor. The mixer output signal obtained at the τ_n is illustrated in Fig. A.5. According to the lock-in amplifier configuration shown in Fig. A.4, the $P_{\text{out}}(\tau_n)$ serves as an input signal to LIA2.

Here, as the LIA2 receives incoming signal from the mixer, an AC gain is applied for amplification,

$$E_{ac_2}(\tau_n) = G_{ac_2}P_{\text{out}}(\tau_n). \quad (\text{A.16})$$

For demodulation purposes, an external reference signal, f_w is obtained from the spinning wheel device (described in Ch. 7 and 8) that is used for modulating the terahertz beam. This signal is used as a reference input signal in the lock-in amplifier for signal demodulation. The external reference signal generated by the spinning wheel can be written as follows:

$$E_w(t) = 1 + V_w \frac{4}{\pi} \left(\sum_{k=1}^{\infty} \frac{\sin((2k-1)\omega_w t + \phi_w)}{(2k-1)} \right). \quad (\text{A.17})$$

Here, $\omega_w = 2\pi f_w$ is the spinning reference frequency with phase, ϕ_w . The PSD of LIA2 produces an output signal that is a product of $E_{ac_2}(\tau_n)$ and $E_w(t)$. Hence, the PSD output is

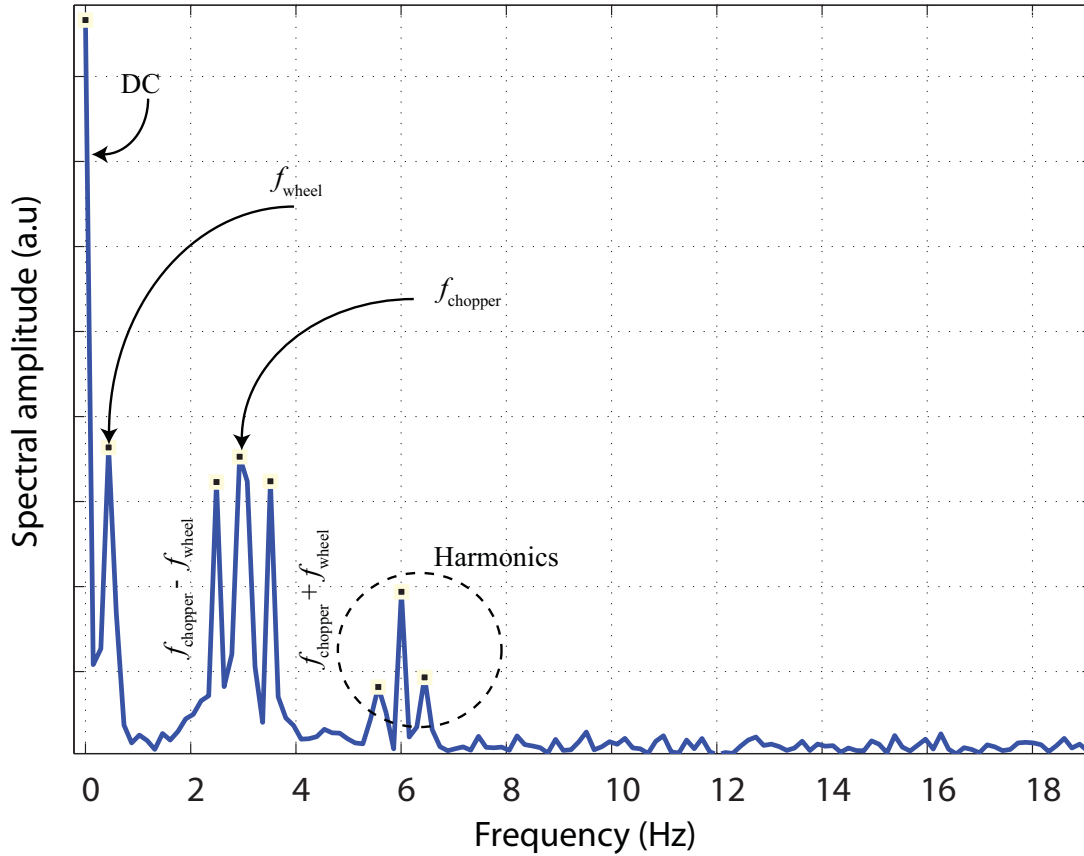


Figure A.5. Simulated mixer output at n th step of the delay stage in frequency domain.

This figure illustrates the product of $X_{\text{modulator}}$ and X_{carrier} channels of the mixer at the n th step of the delay stage in frequency domain. The $X_{\text{modulator}}$ input channel is fed with the simulated double-modulated signal, $E_{s_2}(\tau_n)$ with f_{chopper} of 3 Hz and f_{wheel} of 0.5 Hz and the X_{carrier} input channel is fed with the simulated chopper reference signal, $E_{c_2}(t)$ with f_c of 3 Hz. Thus, the simulated $E_{s_2}(\tau_n)$ consists of a sum component (3 Hz + 0.5 Hz) and a difference component (3 Hz - 0.5 Hz) as illustrated in the figure above. With the assumption that the phase and frequency components of $E_{s_2}(\tau_n)$ synchronises to the phase and frequency components of $E_{c_2}(t)$, one can deduce the output of the mixer, $P_{\text{out}}(\tau_n)$ as shown in the figure. Therefore, the simulated double-modulated signal will be shifted towards the DC at the output of the mixer. The shifted components will then enter the input channel of LIA2 for further demodulation process to produce the amplitude signal.

$$E_{\text{psd}_2}(\tau_n) = E_{\text{ac}_2}(\tau_n)E_w(t) . \quad (\text{A.18})$$

Assuming that the wheel's phase, ϕ_{wheel} , is synchronised to ϕ_w and the wheel frequency, ω_{wheel} is synchronised to ω_w , the amplified signal is further frequency-shifted after the PSD stage. This signal is then low-pass filtered to remove the redundant information and only DC component will be taken into account for DC amplification. Thus, the output signal detected at LIA2 is known as the time delay dependant amplitude signal, $E_{\text{amplitude}}(\tau_n)$.

According to (Mickan *et al.* 2004, Mickan 2003), with the above mean and amplitude signals, one may extract the reference and sample signals according to the following formula:

$$\tilde{E}_{\text{reference}}(\tau_n) = \tilde{E}_{\text{mean}}(\tau_n) + \tilde{E}_{\text{amplitude}}(\tau_n) , \quad (\text{A.19})$$

$$\tilde{E}_{\text{sample}}(\tau_n) = \tilde{E}_{\text{mean}}(\tau_n) - \tilde{E}_{\text{amplitude}}(\tau_n) . \quad (\text{A.20})$$

A.4 Chapter summary

This chapter has described a modelling technique for terahertz signal extraction using the lock-in amplifier. In Sec. A.2, a detailed modelling technique for a standard THz-TDS has been presented. Section A.3 described a detailed modelling technique for double-modulated THz-DTDS. In these modelling work, white noise and $1/f$ noise originating from the slow drifting amplifiers have been considered for demonstration purposes. The modelling techniques presented in this chapter are used extensively in Ch. 7 to model the rapid succession measurement using the spinning wheel.

Terahertz detection of substances



T RAYS have proven to be of great use in the detection of biological and nonmetallic substances that are not readily detected by other means. In many instances, conventional methods of detection (detection of hidden objects or substances within a package), such as X-rays manage only to reveal dense objects, but have difficulties in detecting plastic objects or soft biological materials. T-rays are able to improve on X-rays, due to their ability to detect nonmetallic and nonpolar substances, as well as offering spectroscopy of these substances.

This chapter will look into the use of transmission mode technique to detect various illicit substances in a suitcase. Common materials used in bags and suitcases such as nylon, polycarbonate, and polyethylene are used to sandwich various illicit substances and are scanned by the commercially available Picometrix™ T-Ray 2000 system to obtain spectral data, simulating the probing of a suitcase.

B.1 Introduction

With the current global security standards being constantly upgraded, a method in which to rapidly and non-invasively scan bag and package contents is an ever growing concern. As current imaging techniques have difficulty in scanning and identifying non-metal and biological substances that could be hidden within a bag or a package, the need for detection of these potential hazards becomes increasingly important. Terahertz time-domain spectroscopy (THz-TDS) can provide an efficient method of detecting the substances under test. Biological substances, explosives and narcotics have already been proven to show a distinctive spectral signature under THz-TDS (Wang *et al.* 2003, Fischer *et al.* 2005a, Federici *et al.* 2005, Shen *et al.* 2005, Te *et al.* 2002, Kawase *et al.* 2003), however work is still required to ensure these signatures can be detected within a concealed bag or package, which is explored in this chapter.

B.1.1 Objectives and framework

The work that this chapter aims to express is a proof-of-concept in the use of THz-TDS in secure areas, such as airports, postal agencies and shipping ports to accurately and efficiently identify substances that are hidden inside bags and packages brought into these areas. This is achieved by a number of steps. Firstly, THz spectra of materials found in bags, (for example, plastics and cotton) must be recorded. Then, after the bag or package is scanned, an algorithm along with the previously recorded reference data interrogates the spectral content of the bag or package to determine the contents. For illicit substances the algorithm then flags the bag or package, displays the type of illicit substance detected, and notifies the operator immediately to take action. This chapter is structured as follows: The methodology involved in simulating a suitcase and contents is described in Sec. B.2. A brief description on the PicometrixTM T-ray 2000 experimental setup used in this measurement is given in Sec. B.3. The results and discussion are elaborated in Sec. B.4 followed by conclusion and recommendation in Sec. B.5.

B.2 Methodology

Initially, spectral data from common packing materials are examined for transparency under THz, following which the THz spectrum of the materials are collected. Plastics that are used in common backpacks or suitcases are investigated and tested for transparency and their respective THz spectrum are recorded. Cotton is also tested for transparency to simulate clothing and its THz spectrum is also recorded. The THz spectrum of a given substance can then be recorded for use in an algorithm for detection.

From a cross-sectional angle, bags and suitcases can be viewed as two plastic sheets forming the outer layers, while the contents (for this work, simple clothing) can be simulated by a cotton sheet. This then forms the basis for the simulation of a suitcase and contents (Fig. B.1). A substance can then be laced onto the cotton, and its signature can be recovered if the data from a clean simulation sample is subtracted from the laced sample data. A specialised sample holder is designed and implemented to carefully hold the sample in place and ensure the air gap between the various materials is kept to a minimum. This involves clamping the materials together as tightly as possible. The thickness of the samples is variable, while the width and length of each sample remains as a 50 mm square.

NOTE:
This figure is included on page 147
of the print copy of the thesis held in
the University of Adelaide Library.

Figure B.1. Simulation of a faux suitcase and contents. The faux suitcase showing two plastic outer layers, with cotton sandwiched between, and laced with a substance. Note that the spiral indicates the laced substance. After Ung *et al.* (2006).

B.3 Experimental Setup

The Picometrix™ T-ray 2000 system is shown in Fig. B.2. A Maitai Ti-sapphire femtosecond modelocked laser is used as a source of optical pulses. This laser provides 210 nm (710 - 920 nm) in useable tuning range with over 2.5 W of average power and a pulse width of less than 100 fs at a repetition rate of 80 MHz. Both the THz transmitter and detector utilize Bowtie photoconductive antennas. The sample, along with

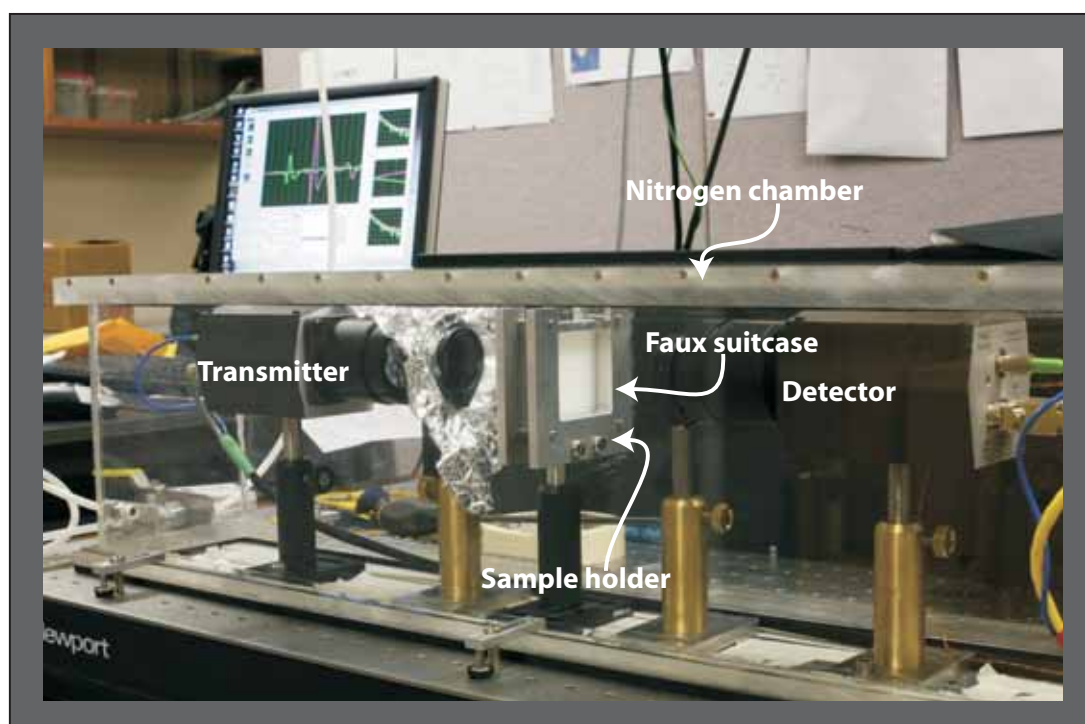


Figure B.2. Picometrix™ T-Ray 2000 spectrometer. This schematic diagram shows a typical Picometrix™ T-Ray 2000 spectrometer. The sample under test is placed at the focal plane.

the transmit and detect heads, is placed within a semi-airtight nitrogen chamber. The chamber is then purged with pure nitrogen to remove water vapour. The purging minimises water lines from appearing in the measured spectrum. This measurement is conducted at room temperature. To ensure the plastics and cotton fit onto the metal sample holder and be pressed together to minimise air gaps, the sheets are cut into 50 mm square pieces with 2 holes drilled into each corner. Two plastic sheets are needed for each sample. The lacing of the cotton is carried out with small amount of α -lactose monohydrate (Sigma-Aldrich Co.), which is mixed into a solution of water and poured

over the cotton sheet to create an even layer of lactose across the cotton. The cotton is then left to dry after which it is placed in between the plastic sheets.

B.4 Results and discussion

In a proof-of-concept experiment, it is shown that T-rays are able to penetrate various common plastics and detect a trace substance laced on a piece of cotton wedged between them. The experiment uses α -lactose, which has distinct terahertz absorption peaks at approximately 0.52 and 1.38 THz (Fig. B.3a). The experiment shows that when a small amount of lactose is laced onto cotton fabric, and then sandwiched between two sheets of the same plastic, the absorption peaks are still readily detectable (Fig. B.3b, red plot). This is opposed to similar lactose-free setup, where no absorption peaks are seen (Fig. A.3b, blue plot).

Two plastic sheets surrounding the cotton appear only to attenuate the absorption peaks and add interface reflection noise as shown in Fig. B.3a and Fig. B.3b. This shows that other organic and non-metal substances may be detectable under similar circumstances.

B.4 Results and discussion

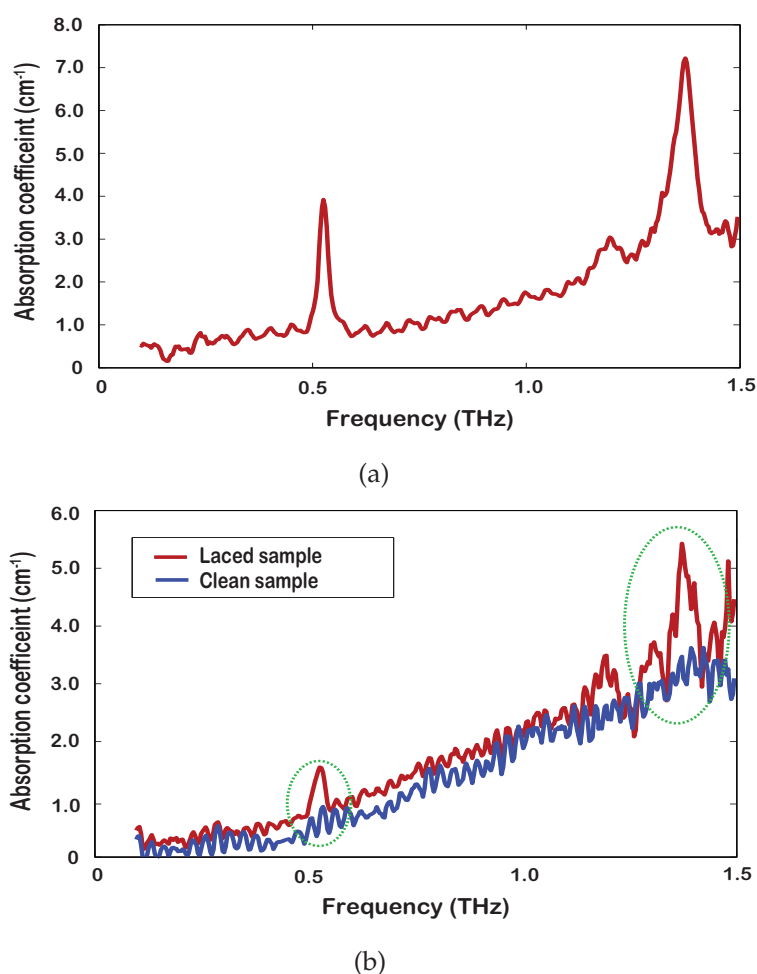


Figure B.3. Absorption curves of α -lactose, clean and laced samples of the faux suitcase.

(a) T-ray absorption spectrum of α -lactose monohydrate at room temperature from 0.1 to 1.5 THz. Distinct peaks can be seen at approximately 0.52 and 1.38 THz, which are unique to α -lactose, showing its distinct T-ray signature. In comparison, (b) shows the T-ray spectrum of a nylon cotton sandwich, with both a clean sample (blue plot) and an α -lactose laced sample (red plot) at room temperature. Two sheets of nylon, each with a thickness of 3.205 mm, were pressed together with a sheet of cotton (0.442 mm thick) in between in order to crudely simulate the profile of a plastic suitcase. The resultant spectra for clean sample shows no signature absorption peaks. Absorption of the T-ray signal is increased with increasing frequencies, as the nylon and cotton absorb the signal to a greater degree. Signal noise and interface reflections can also be seen in the data. The laced sample clearly shows the signature absorption peaks from (a) when the cotton is laced with α -lactose. The circled areas clearly show the absorption peaks at approximately 0.52 and 1.38 THz, which are characteristic to α -lactose, indicating that it is present in this particular sample. After Ung *et al.* (2006).

B.5 Conclusion and recommendation

From these experiments, a proof-of-concept of the use of THz-TDS in secure areas, for the screening and detection of illicit substances in bags and packages, is achievable provided that a library containing spectral signatures of many substances is available and a suitable and accurate algorithm to determine the substances is present. For future work, higher bandwidth T-ray signals would also aid the detection and identification of illicit substances, as this would provide a larger set of unique features due to the wider frequency range. Deeper penetration of bags and packages would also be required, thus greater signal power is needed. If this can be achieved, the possibility of bringing such a machine into reality and use in secure areas is possible.

Appendix C

Experimental Equipment

THE equipment used in the conventional THz-TDS and double-modulated THz-DTDS measurements are described in further detail in this appendix. Data acquisition techniques using LabVIEW™ are discussed in this appendix. The signal analysis technique using MATLAB is covered in Appendix D.

C.1 Conventional THz time-domain spectrometer

Figure C.1 shows the layout of the conventional THz time-domain spectrometer used in our lab. Most of the experimental results presented in this Thesis are obtained from this spectrometer. This section describes the equipment used for implementing the conventional terahertz time-domain spectrometer. The laser system, optical and mechanical components are attached to a vibration proof optical table. Other components such as lock-in amplifier and motion controller are placed under the optical table to avoid tripping. Also, a custom-built nitrogen chamber is attached to the optical table as shown in the figure. This chamber is purged with nitrogen during measurements to minimise the water lines effect.

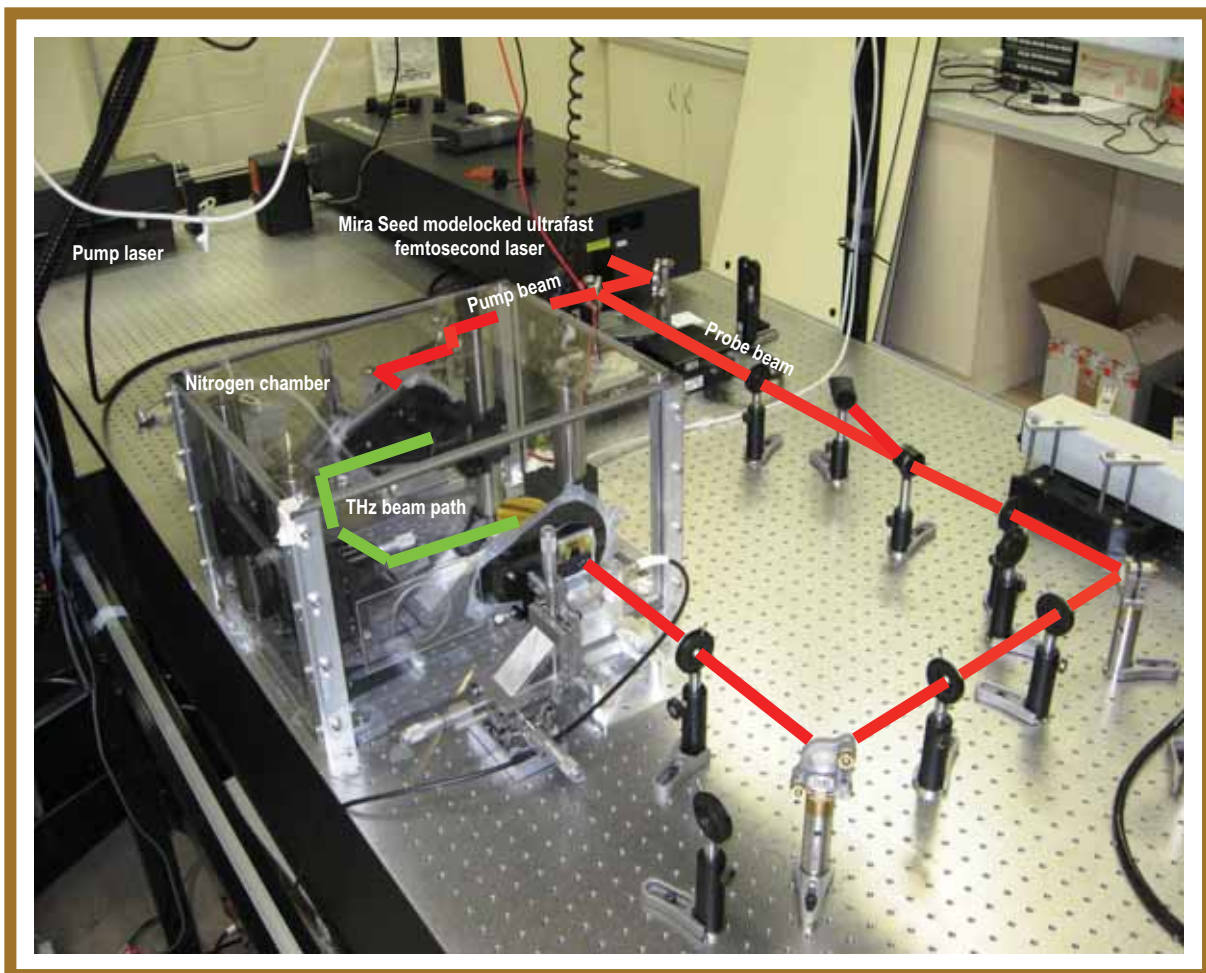


Figure C.1. Conventional terahertz time-domain spectrometer. This figure shows the T-ray spectrometer used for measurements in this thesis. The components used to build this spectrometer are described in the text.

C.1.1 Modelocked femtosecond laser

The laser system used in the above spectrometer for generation and detection of terahertz radiation is known as MiraSeed modelocked ultrafast laser manufactured by Coherent, Inc. (Fig. C.2). This laser uses Titanium: sapphire crystal to produce ultra-short, wide bandwidth, and femtosecond pulses. This laser is used to produce the pump and probe beams to generate and detect terahertz radiation.

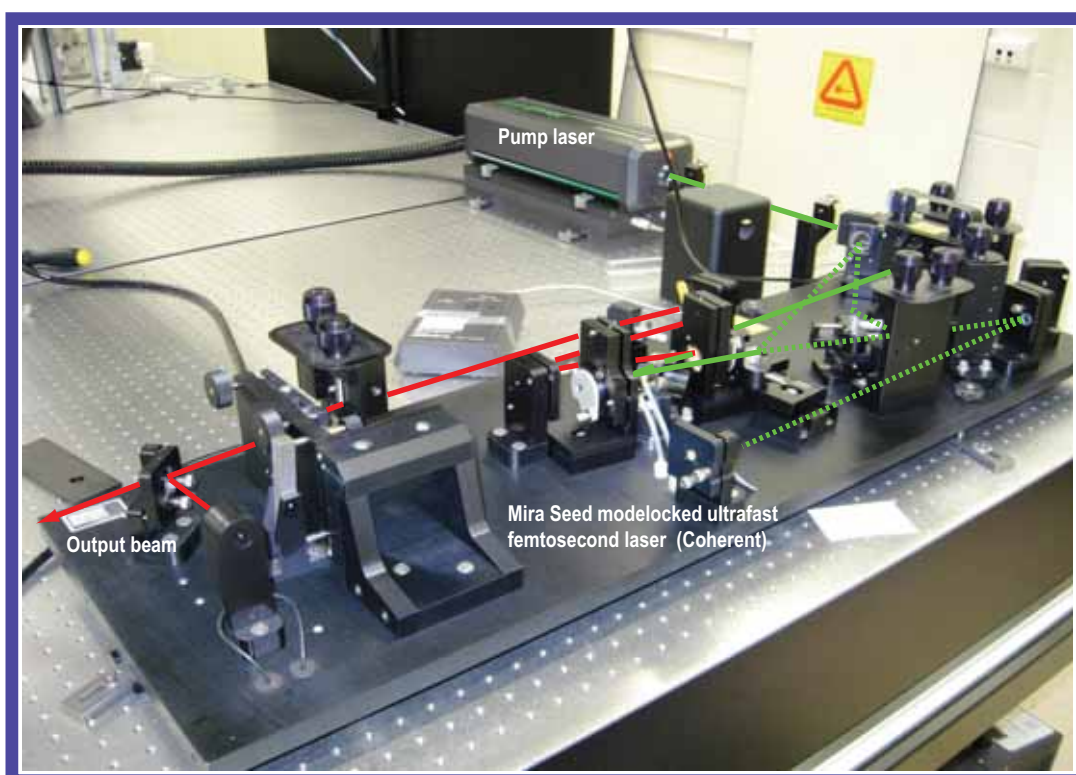


Figure C.2. A MiraSeed Ti-sapphire femtosecond modelocked laser. This photograph shows the interior of Mira Seed modelocked ultrafast femtosecond laser that is used as a source of optical pulses. The Seed is pumped by Verdi V6 laser with a wavelength of 532 nm. The femtosecond laser produces an output pulse duration of 20 fs at a repetition rate of 76 MHz. This laser has an output power of 1 W with a centered wavelength at 800 nm.

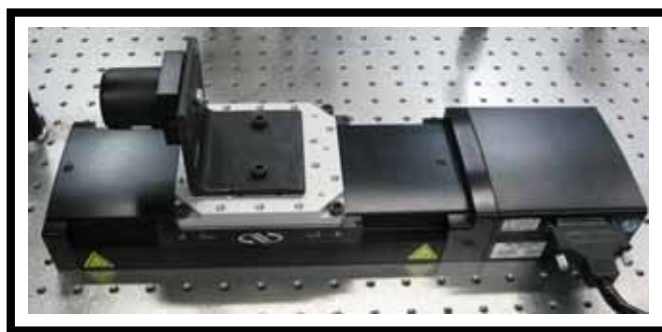
C.1 Conventional THz time-domain spectrometer

C.1.2 XPS Motion controller

Figure C.3 shows a XPS motion controller and a motorised delay stage manufactured by Newport Corporation. These devices are used for gating the THz signal generated through the spectrometer. The motion controller allows high-speed communication through 10/100 Base-T Ethernet and capable of controlling up to 8 axes (i.e., motorised delay stages) concurrently.



(a) XPS Motion Controller



(b) Motorised delay stage

Figure C.3. XPS motion controller and motorised delay stage. This figure depicts the XPS controller used for delaying the motorised delay stage at the pump beam of the T-ray spectrometer. This controller is capable of handling of up to 8 channels and allows high-speed communication through 10/100 Base-T Ethernet connection. Further details can be found in the manufacturer's manual.

C.1.3 Lock-in amplifier configuration

A photograph of a standard Stanford Research System SR830 lock-in amplifier (LIA) used in the T-ray spectrometer is shown in Fig. C.4. The full operational details of LIA model SR830 can be found from the manufacturer's manual. In a nutshell, the SR830 LIA is used to demodulate the incoming terahertz signal from the detector with an appropriate reference signal. There are two main parts to the operation of this lock-in amplifier: first, the demodulation process at a Phase Sensitive Detector (PSD) and second, filtering at a narrow band low pass filter (LPF). In a conventional terahertz time domain spectrometer, the lock-in amplifier uptakes two input signals; an input signal (terahertz signal) and a reference signal (chopper signal). These signals are then multiplied to produce sum ($2f$) and difference components (DC). With an assumption that both the input and reference signals are synchronised in both frequency and phase, the narrowband low pass filter will attempt to filter any frequency component above the DC. The SR830 allows narrow bandwidth selection and this can be achieved by increasing the time constant. According to the manufacturer's manual, the relationship between the filter bandwidth and the LIA time constant can be written as follows:

$$BW_{LIA} = \frac{1}{S \times T} \quad (C.1)$$

where T represents the lock-in amplifier's time constant and S refers to the slope of the filter. This lock-in amplifier allows slope settings of 6 db/octave, 12 db/octave, 18 db/octave, and 24 db/octave. Therefore, the dc output obtained at the output channel of the LIA is transferred to the computer for signal capturing and data analysis. The principles of operation of lock-in amplifier in demodulating the terahertz signal is described through simulation technique in Appendix. A.



Figure C.4. Photograph of SR830 lock-in amplifier. This figure shows the photograph of the SR830 model lock-in amplifier.

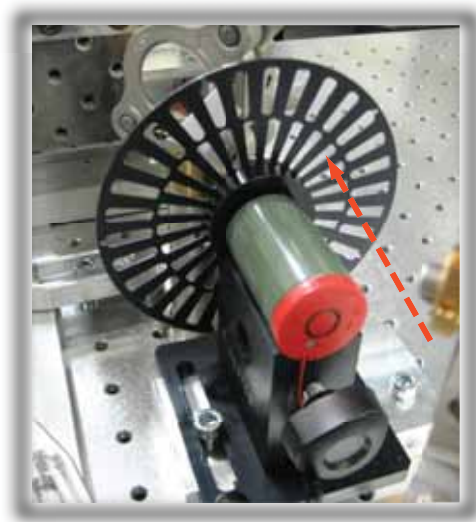
C.1 Conventional THz time-domain spectrometer

C.1.4 SR540 chopper controller

Figure C.5 depicts the SR540 chopper controller and the chopper device used for modulating the optical beam and also as an external reference signal to the lock-in amplifier. The controller shown in Fig. C.5a allows chopping frequency of up to 4 kHz. Figure C.5b shows the chopper wheel used to interrupt the optical beam. The chopper wheel is equally spaced to provide 50% duty cycle. The chopper wheel is placed at pump beam of the spectrometer.



(a) SR540 Chopper controller



(b) Chopper wheel

Figure C.5. SR540 Chopper system. This figure illustrates the SR540 chopper system composed of a chopper controller and a chopper wheel. This system is capable of handling chopping frequency of up to 4 kHz.

C.1.5 Optical components

This section describes the optical components used in the terahertz setup described in Chapter 3. These components are commercially available from standard optics suppliers (i.e., Newport Corp., Thorlabs).

Mirrors and lens

A number of pyrex mirrors with high surface quality and broadband coating for the ultrafast 800 nm pulses are used. These mirrors are mainly used for reflecting the laser beam. These mirrors are 25.4 mm in diameter that is sufficiently wide to handle the optical beam size. Since the photoconductive antennas used in the spectrometer operate at low power, neutral density (ND) filters are required to filter the laser output power. Optical lenses are also used in our terahertz setup. These lenses are used for focusing the optical beam into the photoconductive antennas to generate THz pulse. Moreover, a gold-plated retroreflector mounted on a delay stage is used to adjust the path length. A 50:50 antireflection beam splitter for splitting the laser pulses into pump and probe beams is also used in our setup. Gold-coated parabolic mirrors are used for collimating and focusing T-rays.

C.1.6 Mechanical components

The XYZ stages and the custom-built photoconductive antenna mounts are considered to be the mechanical components for the terahertz spectrometer apart from the motorised delay stage and the optical chopper wheel described in the above sections. The function of the XYZ stage is to hold the optical lens and adjust in the XYZ direction. The XYZ stage plays an important role in optimising the system's bandwidth.

The custom-built photoconductive antenna mounts are depicted in Fig. 3.9. These mounts are specially designed to hold the photoconductive antennas described in Ch. 3. The main body of the mount is made from aluminium. According to Fig. 3.9, the photoconductive antenna is placed on the antenna slider that moves in a single direction. For coupling and collimation purposes, a Si hyperhemispherical lens is attached to the back of the photoconductive antenna as shown in the Fig. 3.9. Here, a custom-made finger mounted on a XY stage is used to hold the Si hyperhemispherical lens.

C.2 Data acquisition for conventional THz-TDS

The THz-TDS spectrometer described in this Thesis is controlled by using a graphical tool called LabVIEW™ version 8.5. This tool is mainly used for controlling the motion controller that moves the delay stage and collects the terahertz signal from the lock-in amplifier. Here, in order to achieve high speed communication, the motion controller is connected to the computer terminal through 10/100 Base-T Ethernet. On the other hand, a General Purpose Interface Bus (GPIB) card and a GPIB cable are required for establishing communication between the lock-in amplifier and the computer terminal. Figure C.6 shows a screen shot of a LabVIEW program for a THz-TDS transmission spectrometer. This program was originally written by Matthias Hoffmann from the University of Freiburg, however, a slight modification has been made to meet the desired functionality.

Features of this program are as follows:

- Input parameter - Users can insert desired parameters such as number of steps, step size, and number of scans.
- File name labelling and browsing.
- Lock-in parameter - Users can set the sensitivity, time constant, GPIB address, and input configuration.
- Time - The expected time to finish the scan.
- View of live temporal shape, spectral amplitude, and saved spectra.
- Automatic save to disk function

The program plots the temporal profile and saves it for analysis. The analysis is carried out using Matlab software program described in the Appendix D (see Sec. D.1).

C.3 Double-modulated THz-DTDS spectrometer

The double-modulated THz-DTDS is implemented based on the conventional THz-TDS without modification on the hardware. However, slight change in the method of signal extraction and data acquisition is required. In this section, the equipment used and the method of signal extraction are described.

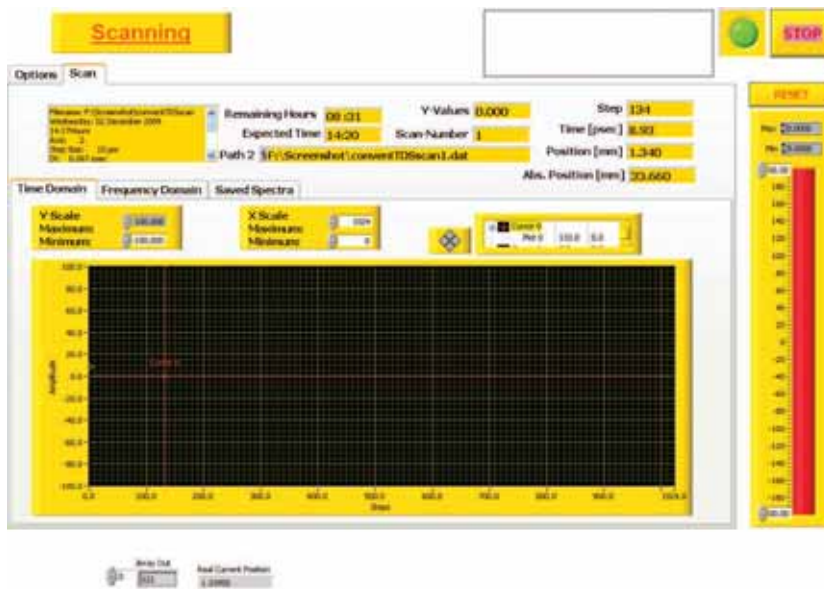


Figure C.6. Screen shot of the LabVIEW program for conventional THz-TDS spectrometer. This program was developed to control the motion controller and acquired terahertz data from the lock-in amplifier. The 'Options' tab is used to insert parameters to control the motion controller and the lock-in amplifier (not shown in the figure). A live view of the temporal profile, spectral amplitude, and saved spectra can be attained from the graph indicator shown above.

C.3 Double-modulated THz-DTDS spectrometer

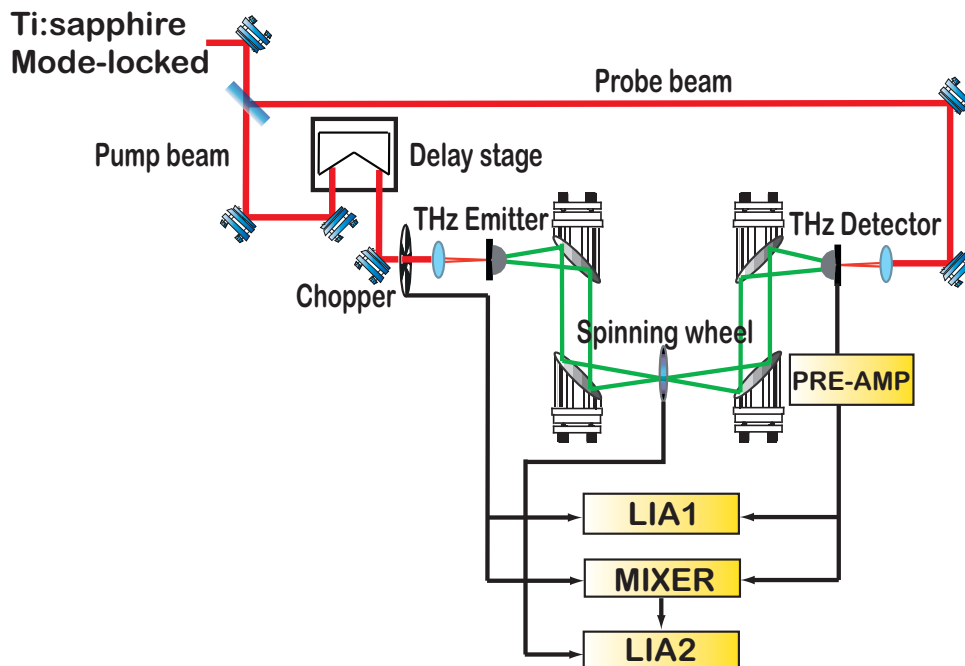


Figure C.7. Double-modulated THz-DTDS spectrometer. This figure shows the schematic diagram of the double-modulated THz-DTDS spectrometer. The spectrometer is widely used for measurements of polymer materials and liquids presented in Ch. 7 and Ch. 8. The incoming femtosecond laser is split into pump and probe beam using a beam splitter which will then go through optics for generating and detecting the THz signal. The spinning wheel is placed in the THz beam and modulated at certain speed.

C.3.1 Double-modulated THz-DTDS

Figure C.7 illustrates the double-modulated THz-DTDS schematic diagram. In a conventional THz-TDS two separate mechanical delay scans are required to obtain the reference and sample pulses, however, in this technique, only one mechanical delay scan is required for obtaining the reference and sample pulses. This can be achieved by introducing the spinning wheel device and dual lock-in amplifier configuration.

C.3.2 Dual lock-in amplifier configuration

The double-modulated signal obtained from the above spectrometer is fed into the lock-in amplifier configuration shown in Fig. C.8. This configuration consists of a SR560 preamplifier, two power splitters, a custom-built mixer, and two SR830 lock-in amplifiers. The preamplifier is used to scale the output level from the THz detector to ensure that the signal entering the lock-in amplifiers is detectable. The power splitters

are used to split the amplified double-modulated signal and the chopper frequency while the mixer is used for demodulating the double-modulated signal at a chopper reference frequency. Here, the mixer is designed without a filter. The lock-in amplifiers are used to extract the mean and amplitude signals.

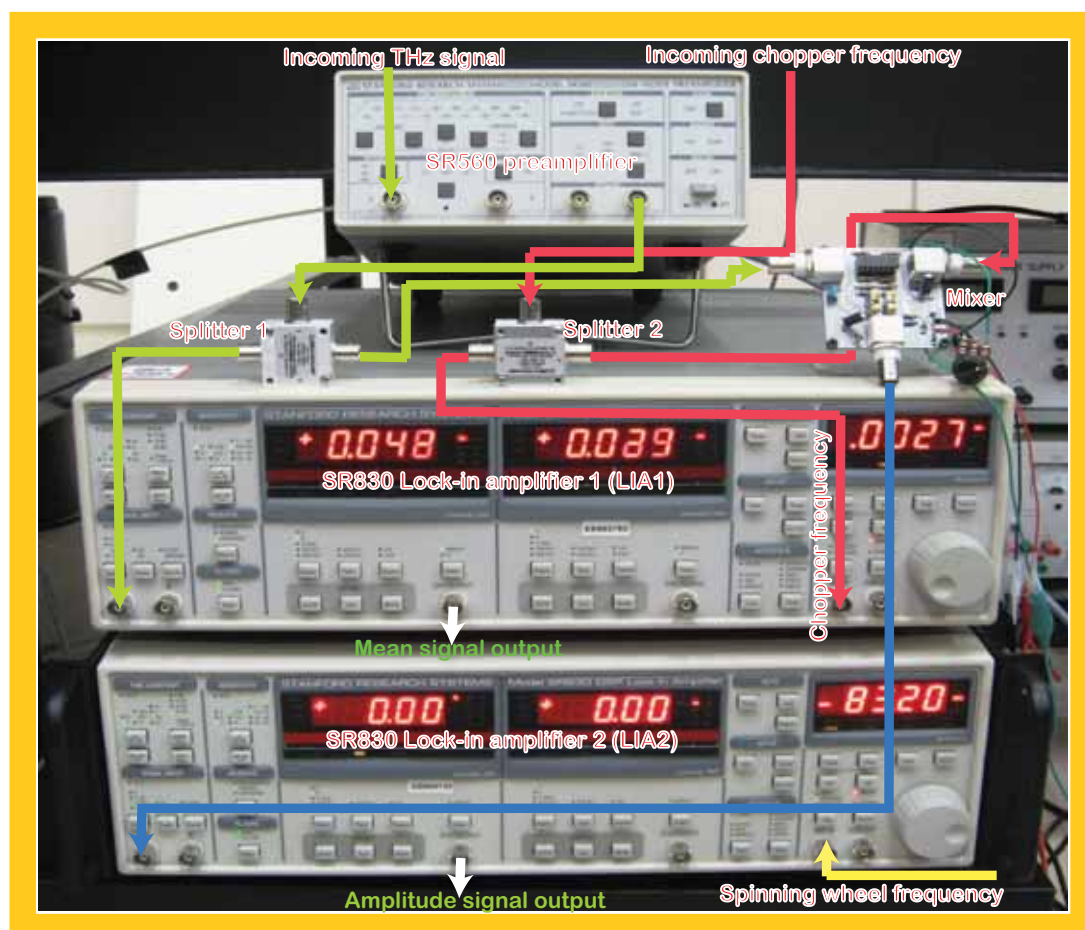


Figure C.8. Dual lock-in amplifier configuration. This photograph shows the lock-in amplifiers configuration for mean and amplitude signals extraction.

C.3.3 Spinning wheel

A novel custom-built spinning wheel device is depicted in Fig. C.9. The spinning wheel technique enables a rapid succession of measurements between the reference and sample signals with a single mechanical delay scan. The main body of the spinning wheel is made from aluminium. The sample holder is made from a stainless-steel material to avoid contamination. A high speed brushless motor is attached to this device for spinning purposes. A photointerrupter circuit and an interrupter disc are designed and

C.4 Data acquisition for double-modulated THz-DTDS

attached at the back of device. This circuit and disc are used to convert the spinning speed in revolution per minute (rpm) into frequency (Hz).

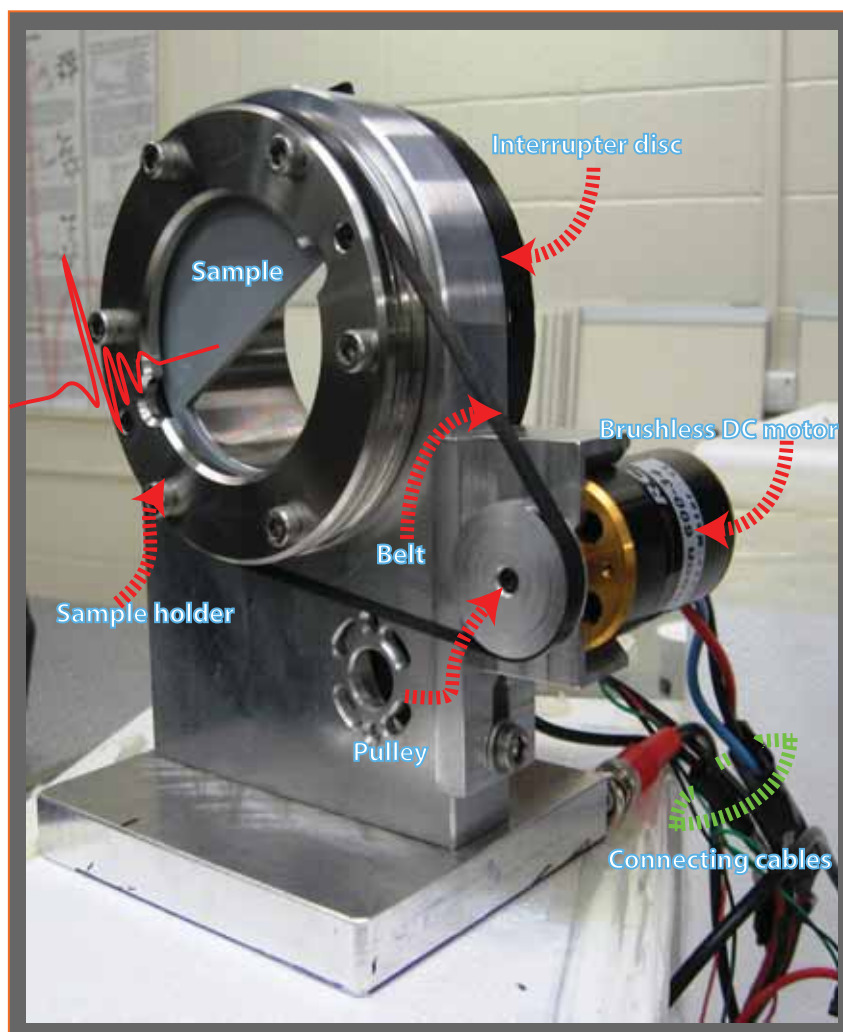


Figure C.9. The spinning wheel prototype. This figure depicts the spinning wheel device used for polymer material and liquid measurements discussed in Ch. 7 and 8.

C.4 Data acquisition for double-modulated THz-DTDS

Figure C.10 shows a screen shot of a LabVIEW program used to control a single motion controller and acquire terahertz signals (mean and amplitude signals) from two lock-in amplifiers simultaneously. The motion controller is connected to the computer terminal through the 10/100 Base-T Ethernet and the lock-in amplifiers are connected to the computer terminal through GPIB ribbon cable. The functionality of this program is similar to the one used in the conventional THz-TDS spectrometer, however,



Figure C.10. Screen shot of LabVIEW program for double-modulated THz-DTDS spectrometer. This is a screen shot of the LabVIEW program developed to control the double-modulated THz-DTDS spectrometer. With this program, one may acquire mean and amplitude data simultaneously for analysis purposes. The graph indicators for acquiring the mean and amplitude signals are shown in the figure.

C.4 Data acquisition for double-modulated THz-DTDS

this program is modified to acquire mean and amplitude data simultaneously from the lock-in amplifiers. The data collected is then analysed using the Matlab software program described in Appendix D (see Sec. D.2).

Appendix D

Matlab Algorithms

THIS appendix presents some of the Matlab algorithms used in this thesis. These algorithms are available as m-files on the attached DVD-ROM. Examples of raw data files used in these algorithms are also attached.

D.1 Conventional THz-TDS analysis program

```
1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 % Program to analyse THz raw data. This program is written to extract THz %
3 %     material parameters through reference and sample signals.           %
4 %                                                                           %
5 % Jegathisvaran Balakrishnan                                             %
6 % The University of Adelaide                                             %
7 % December 2009                                                         %
8 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
9
10 clear all;
11 c = 3E8;% Speed of light
12 d = 3E-3;% Thickness of the sample to be measured
13 Nscan = 6;% Number of scans
14 step=1024;% Number of steps for each scan
15
16 refmatrix_amp(step,Nscan) = 0;      % Intialize all the variables to zero %
17 refmatrix_time(step,Nscan) = 0;     %                                     %
18 sammatrix_amp(step,Nscan) = 0;      %                                     %
19 sammatrix_time(step,Nscan) = 0;     %                                     %
20 mean_smatrix_amp = 0;               %                                     %
21 mean_sammatrix_time = 0;            %                                     %
22 mean_rmatrix_amp = 0;               %                                     %
23 mean_refmatrix_time = 0;            %                                     %
24 mean_sample_absolute = 0;           %                                     %
25 mean_reference_absolute = 0;        %                                     %
26 mean_normal_phase = 0;              %                                     %
27 mean_match_phase = 0;               %                                     %
28 mean_transmission_absolute = 0;     %                                     %
29 mean_refractive_index = 0;          %                                     %
30 mean_absorption = 0;                %                                     %
31 standard_dev_refrac = 0;            %                                     %
32 standard_dev_absorp = 0;            %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
33
34 for N = 1:Nscan
35     %Import reference files for reading only
36     disp(['Running reference ' int2str(N)]);
37     fid = fopen(['reference_airtight' int2str(N) '.dat'],'r');
38     reference_scan = textscan(fid,'%f %f ','headerlines',2);
39     refmatrix_amp(:,N)= reference_scan{: ,2};
40     refmatrix_time(:,N) = reference_scan{: ,1};
```

```
41     fclose(fid);
42
43     %Import sample files for reading only
44     disp(['Running sample ' int2str(N)]);
45     fid2 = fopen(['sample_80um' int2str(N) '.dat'],'r');
46     reference_scan2 = textscan(fid2,'%f %f','headerlines',2);
47     sammatrix_amp(:,N) = reference_scan2{: ,2};
48     sammatrix_time(:,N) = reference_scan2{: ,1};
49     fclose(fid2);
50
51     zero_offsetA(:,N) = mean(refmatrix_amp(1:10,N));
52     Rmatrix_amp(:,N) = refmatrix_amp(:,N)-zero_offsetA(:,N);
53     zero_offsetB(:,N) = mean(sammatrix_amp(1:10,N));
54     Smatrix_amp(:,N) = sammatrix_amp(:,N)-zero_offsetB(:,N);
55     rmatrix_amp(:,N) = Rmatrix_amp(:,N);% Nth reference
56     smatrix_amp(:,N) = Smatrix_amp(:,N);% Nth sample
57
58     % Zero padding if it is necessary
59     % for matupdateb=400:512
60     %   rmatrix_amp(matupdateb,N) = 0;
61     % end
62     %
63     % for matupdatea=400:512
64     %   smatrix_amp(matupdatea,N) = 0;
65     % end
66     [m,n] = size(sammatrix_amp(:,1));
67     timestep = mean(diff(sammatrix_time(1:m)));
68     frequency = [0:m-1]'/timestep/m;
69
70     % FFT of the reference and sample signals
71     sample_fft(:,N) = fft(smatrix_amp(:,N));
72     sample_absolute(:,N) = abs(sample_fft(:,N));
73     reference_fft(:,N) = fft(rmatrix_amp(:,N));
74     reference_absolute(:,N) = abs(reference_fft(:,N));
75
76     % Transmission coefficient
77     transmission(:,N) = sample_fft(:,N)./reference_fft(:,N);
78     % The second element of the frequency gives the resolution.
79     resolution = frequency(2);
80
81     transmission_absolute(:,N) =abs(transmission(:,N));
82
```

D.1 Conventional THz-TDS analysis program

```
83 % Unwrap the transmission angle followed by phase extrapolation
84 % for phase information extraction
85 transmission_phase(:,N) = -unwrap(angle(transmission(:,N)));
86 normal_phase(:,N) = transmission_phase(:,N);
87 lower_frequency = ceil(0.2/resolution);
88 upper_frequency = floor(0.45/resolution);
89 phase_difference(1,N) = transmission_phase(upper_frequency,N)
90 -transmission_phase(lower_frequency,N);
91
92 slope(1,N) = phase_difference(1,N)/(frequency(upper_frequency)
93 -frequency(lower_frequency));
94 yAxis(:,N) = slope(1,N)*frequency(1:lower_frequency);
95 j(1,N) = slope(1,N)*frequency(lower_frequency);
96 j2(1,N) = transmission_phase(lower_frequency,N);
97 diffj(1,N) = j(1,N)-j2(1,N);
98 a(:,N) = [yAxis(:,N)];
99 b(:,N) = [transmission_phase(lower_frequency+1:m,N)+diffj(1,N)];
100 match_phase(:,N) = [a(:,N); b(:,N)];% combining the a and b into matrix
101
102 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
103 % (1)Refractive index, extinction and absorption coefficient analysis %
104 %           for dual-thickness geometry                               %
105 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
106
107 % omega = 2*pi*frequency*1*10^12;
108 % refractive_index(:,N) = c./(d.*omega).*match_phase(:,N)+1;
109 % extinction(:,N) = (c./(d*omega)').*log(transmission_absolute(:,N)');
110 % absorption_coefficient(:,N) = -(2/d)*log(transmission_absolute(:,N)');
111 % absorption(:,N) = absorption_coefficient(:,N)/100;
112
113 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
114 % (2)Refractive index, extinction and absorption coefficient analysis %
115 %           for air reference and sample (Used in Ch.4 and 5)         %
116 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
117
118 % omega = 2*pi*frequency*1*10^12;
119 % refractive_index(:,N) = 1+(c*match_phase(:,N)./(d*omega));
120 % absorption_coefficient(:,N) = -(2/d)*log((1+refractive_index(:,N))
121 % .*(1+refractive_index(:,N)).*transmission_absolute(:,N)./
122 % (4.*refractive_index(:,N))));
123 % absorption(:,N) = absorption_coefficient(:,N)/100;
124
```

```

125 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
126 % (3)Refractive index, extinction and absorption coefficient analysis %
127 %       for measurements with cell (transmission geometry (i))      %
128 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
129
130 % omega = 2*pi*frequency*1*10^12;
131 % refractive_index(:,N) = 1+(c*match_phase(:,N)./(d*omega));
132 % absorption_coefficient(:,N) = -(2/d)*log((1.53+refractive_index(:,N))
133 % .* (1.53+refractive_index(:,N)).*transmission_absolute(:,N)./(6.4009.
134 % *refractive_index(:,N)));
135 % absorption(:,N) = absorption_coefficient(:,N)/100;
136
137
138 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
139 % (4)Refractive index, extinction and absorption coefficient analysis %
140 %       for measurements with cell with air tight reference          %
141 %                               (transmission geometry (ii))          %
142 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
143
144 omega = 2*pi*frequency*1*10^12;
145 refractive_index(:,N) = c*match_phase(:,N)./(d*omega);
146 absorption_coefficient(:,N) = -(2/d)*log((1.53+refractive_index(:,N)).
147 *(1.53+refractive_index(:,N)).*transmission_absolute(:,N)./
148 (6.12.*refractive_index(:,N)));
149 absorption(:,N) = absorption_coefficient(:,N)/100;
150
151 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
152 %       Plot the temporal shape of the reference and sample signals  %
153 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
154
155 graph_one = figure(1);
156 subplot(2,1,1);
157 plot(sammatrix_time(:,N),smatrix_amp(:,N),'b','linewidth',1);
158 hold on
159 plot(refmatrix_time(:,N),rmatrix_amp(:,N),'b','linewidth',1);
160 grid on
161 xlabel('Time (ps)');
162 ylabel('Amplitude (a.u)');
163
164 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
165 %       Plot the spectral amplitude of the reference and sample signals %
166 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```


D.1 Conventional THz-TDS analysis program

```
167
168     subplot(2,1,2);
169     semilogy(frequency(1:m/2),reference_absolute(1:m/2,N),'b','linewidth',1);
170     hold on
171     semilogy(frequency(1:m/2),sample_absolute(1:m/2,N),'b','linewidth',1);
172     grid on
173     xlabel('Frequency (THz)');
174     ylabel('Spectral amplitude (a.u)');
175
176     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
177     %           Plot the original and extrapolated phase information           %
178     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
179
180     graph_two = figure(2);
181     subplot(2,1,1);
182     plot(frequency(1:m/2),normal_phase(1:m/2,N),'b','linewidth',1);
183     hold on
184     plot(frequency(1:m/2),match_phase(1:m/2,N),'g','linewidth',1);
185     grid on
186     xlabel('Frequency (THz)');
187     ylabel('Phase (rad)');
188
189     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
190     %           Plot the transmission coefficient                               %
191     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
192
193     transmission_absolute(:,N) = transmission_absolute(:,N)*100;
194     subplot(2,1,2);
195     plot(frequency(1:m/2),transmission_absolute(1:m/2,N),'b','linewidth',1);
196     hold on
197     grid on
198     xlabel('Frequency (THz)');
199     ylabel('Transmission (%)');
200
201     graph_three = figure(3);
202     subplot(2,1,1);
203     plot(frequency(1:m/2),refractive_index(1:m/2,N),'b','linewidth',1);
204     grid on
205     xlabel('Frequency (THz)');
206     ylabel('refractive index (n)');
207
208     subplot(2,1,2);
```

```
209     plot(frequency(1:m/2),absorption(1:m/2,N),'b','linewidth',1);
210     grid on
211     xlabel('Frequency (THz)');
212     ylabel('Absorption coefficient (\alpha)');
213 end
214
215 mean_smatrix_amp = mean(smatrix_amp,2);
216 mean_sammatrix_time = mean(sammatrix_time,2);
217 mean_rmatrix_amp = mean(rmatrix_amp,2);
218 mean_refmatrix_time = mean(refmatrix_time,2);
219 mean_sample_absolute = mean(sample_absolute,2);
220 mean_reference_absolute = mean(reference_absolute,2);
221 mean_normal_phase = mean(normal_phase,2);
222 mean_match_phase = mean(match_phase,2);
223 mean_transmission_absolute = mean(transmission_absolute,2);
224 mean_refractive_index = mean(refractive_index,2);
225 mean_absorption = mean(absorption,2);
226 standard_dev_refrac = std(refractive_index,0,2);
227 standard_dev_absorp = std(absorption,0,2);
228 standard_dev_ref = std(rmatrix_amp,0,2);
229
230 % Plot the averaged terahertz reference and sample pulses in time domain.
231 graph_one = figure(1);
232     subplot(2,1,1);plot(mean_refmatrix_time(1:m),mean_rmatrix_amp(1:m),'r',
233         'linewidth',2);
234     hold on
235     plot(mean_refmatrix_time(1:m),mean_smatrix_amp(1:m),'g','linewidth',2);
236     grid on
237     legend('Reference','Sample',1);
238     title('Temporal pulse shape for xxxx');
239     xlabel('Time (ps)');
240     ylabel('Amplitude (a.u)');
241
242 % Plot the averaged spectral amplitude in frequency domain.
243     subplot(2,1,2);
244     semilogy(frequency(1:m/2),mean_reference_absolute(1:m/2),'r','linewidth',2);
245     hold on
246     semilogy(frequency(1:m/2),mean_sample_absolute(1:m/2),'g','linewidth',2);
247     grid on
248     legend('Reference','Sample',1);
249     title('Spectral amplitude for xxxx');
250     xlabel('Frequency (THz)');
```

D.1 Conventional THz-TDS analysis program

```
251     ylabel('Spectral amplitude (a.u)');
252
253 % Plot the averaged original and extrapolated phases in frequency domain.
254 graph_two = figure(2);
255     subplot(2,1,1);
256     plot(frequency(1:m/2),mean_normal_phase(1:m/2),'b','linewidth',2);
257     hold on
258     plot(frequency(1:m/2),mean_match_phase(1:m/2),'c','linewidth',2);
259     grid on
260     legend('Original','Extrapolated',1);
261     title('Phase in frequency domain');
262     xlabel('Frequency (THz)');
263     ylabel('Phase (rad)');
264
265 % Plot the averaged transmission coefficient in frequency domain.
266     subplot(2,1,2);
267     plot(frequency(1:m/2),mean_transmission_absolute(1:m/2),'r','linewidth',1);
268     grid on
269     title('Transmission coefficient—absolute value (%)');
270     xlabel('Frequency (THz)');
271     ylabel('Transmission (%)');
272
273 % Plot the averaged, smoothed, and errorbar of the refractive index in
274 % frequency domain.
275 graph_three = figure(3);
276     subplot(2,1,1);
277     plot(frequency(1:m/2),mean_refractive_index(1:m/2),'r','linewidth',2);
278     hold on
279     for s = 1:(m-2)
280         average_REF(s) = mean((mean_refractive_index(s)
281             +mean_refractive_index(s+1))/2);
282     end
283     errorbar(frequency(1:10:m/6),mean_refractive_index(1:10:m/6),
284         standard_dev_refrac(1:10:m/6),'k','linewidth',1.5);
285     hold on
286     plot(frequency(1:m-2),average_REF(1:m-2),'g','linewidth',2);
287     grid on
288     title('Refractive index of xxxx ');
289     legend('Original','Error bar','Smoothed',1)
290     xlabel('Frequency (THz)');
291     ylabel('Refractive index (n)');
292
```

```

293 % Plot the averaged, smoothed, and errorbar of the absorption coefficient in
294 % frequency domain.
295     subplot(2,1,2);
296     plot(frequency(1:m/2),mean_absorption(1:m/2),'r','linewidth',1);
297     hold on
298     for s = 1:(m-2)
299         average_abs (s) = mean((mean_absorption(s)+mean_absorption(s+1))/2);
300     end
301     errorbar(frequency(1:14:m/6),mean_absorption(1:14:m/6),
302     standard_dev_absorp(1:14:m/6),'k','linewidth',2);
303     hold on
304     plot(frequency(1:m-2),average_abs(1:m-2),'g','linewidth',2);
305     grid on
306     title('Absorption coefficient of')
307     legend('Original','Errorbar','Smoothed',1)
308     xlabel('Frequency (THz)');
309     ylabel('Absorption coefficient (\alpha)');
310
311 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
312 %                               End of the program                               %
313 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

D.2 Double-modulated THz-DTDS analysis program

```

1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 % Program to analyse double-modulated THz-DTDS raw data. The program is %
3 % written to analyse mean and amplitude raw data obtained from the %
4 % double-modulated THz-DTDS measurements. The graphs for polymer %
5 % measurements and liquid measurements presented in Ch. 7 and Ch. 8 are %
6 % based on this program. %
7 % %
8 % Jegathisvaran Balakrishnan %
9 % The University of Adelaide %
10 % December 2009 %
11 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
12
13 clear all;
14 c = 3E8; % Speed of light.
15 d = 80E-6; % Thickness of the sample to be measured.
16 Nscan = 10; % Number of scans.
17 step=512; % Number of steps for each scan.
18

```

D.2 Double-modulated THz-DTDS analysis program

```
19 refmatrix_amp(step,Nscan) = 0; % Intialize all the variables to zero.%
20 refmatrix_time(step,Nscan) = 0; %
21 sammatrix_amp(step,Nscan) = 0; %
22 sammatrix_time(step,Nscan) = 0; %
23 mean_smatrix_amp = 0; %
24 mean_sammatrix_time = 0; %
25 mean_rmatrix_amp = 0; %
26 mean_refmatrix_time = 0; %
27 mean_sample_absolute = 0; %
28 mean_reference_absolute = 0; %
29 mean_normal_phase = 0; %
30 mean_match_phase = 0; %
31 mean_transmission_absolute = 0; %
32 mean_refractive_index = 0; %
33 mean_absorption = 0; %
34 standard_dev_refrac = 0; %
35 standard_dev_absorp = 0; %
36 test = 0; %
37 test_real = 0; %
38 test_imag = 0; %
39 test_index = 0; %
40 test_alphax = 0; %
41 test_alpha = 0; %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
42
43 % Importing measurement scans for analysis.
44 for N = 1:Nscan
45     % Import mean files for reading only.
46     disp(['Running mean ' int2str(N)]);
47     fid = fopen(['Mean' int2str(N) '.dat'],'r');
48     reference_scan = textscan(fid,'%f %f','headerlines',2);
49     refmatrix_amp(:,N)= reference_scan{: ,2};
50     refmatrix_time(:,N) = reference_scan{: ,1};
51     fclose(fid);
52
53     % Import amplitude files for reading only.
54     disp(['Running amplitude ' int2str(N)]);
55     fid2 = fopen(['Amplitude' int2str(N) '.dat'],'r');
56     reference_scan2 = textscan(fid2,'%f %f','headerlines',2);
57     sammatrix_amp(:,N) = reference_scan2{: ,2};
58     sammatrix_time(:,N) = reference_scan2{: ,1};
59     fclose(fid2);
60
```

```

61 % Introducing offset.
62 zero_offsetA(:,N) = mean(refmatrix_amp(1:20,N));
63 Rmatrix_amp(:,N) = refmatrix_amp(:,N)-zero_offsetA(:,N);
64
65 zero_offsetB(:,N) = mean(sammatrix_amp(1:20,N));
66 Smatrix_amp(:,N) = sammatrix_amp(:,N)-zero_offsetB(:,N);
67
68 % Calculating reference and sample signal through mean and amplitude raw
69 % data.
70 rmatrix_amp(:,N) = Rmatrix_amp(:,N) + Smatrix_amp(:,N);
71 smatrix_amp(:,N) = Rmatrix_amp(:,N) - Smatrix_amp(:,N);
72
73 [m,n] = size(sammatrix_amp(:,1));
74 timestep = mean(diff(sammatrix_time(1:m)));
75 frequency = [0:m-1]'/timestep/m;
76 sample_fft(:,N) = fft(smatrix_amp(:,N));
77 sample_absolute(:,N) = abs(sample_fft(:,N));
78 reference_fft(:,N) = fft(rmatrix_amp(:,N));
79 reference_absolute(:,N) = abs(reference_fft(:,N));
80
81 % Transmission coefficient
82 transmission(:,N) = sample_fft(:,N)./reference_fft(:,N);
83
84 % The second element of the frequency gives the resolution.
85 resolution = frequency(2);
86
87 transmission_absolute(:,N) =abs(transmission(:,N));
88
89 % Unwrap the transmission angle for phase.
90 transmission_phase(:,N) = -unwrap(angle(transmission(:,N)));
91 normal_phase(:,N) = transmission_phase(:,N);
92
93 % Determine the lower frequency element.
94 lower_frequency = ceil(0.2/resolution);
95
96 % Determine the upper frequency element.
97 upper_frequency = floor(0.5/resolution);
98
99 % Phase extrapolation.
100 phase_difference(1,N) = transmission_phase(upper_frequency,N)
101 -transmission_phase(lower_frequency,N);
102 slope(1,N) = phase_difference(1,N)/(frequency(upper_frequency)

```

D.2 Double-modulated THz-DTDS analysis program

```
103     -frequency(lower_frequency));
104     yAxis(:,N) = slope(1,N)*frequency(1:lower_frequency);
105     j(1,N) = slope(1,N)*frequency(lower_frequency);
106     j2(1,N) = transmission_phase(lower_frequency,N);
107     diffj(1,N) = j(1,N)-j2(1,N);
108     a(:,N) = [yAxis(:,N)];
109     b(:,N) = [transmission_phase(lower_frequency+1:m,N)+diffj(1,N)];
110     match_phase(:,N) = [a(:,N); b(:,N)];
111
112     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
113     %   Refractive index, extinction and absorption coefficient analysis   %
114     %   for reference and sample (dual-thickness liquid measurement).   %
115     %                                                                 %
116     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
117
118     omega = 2*pi*frequency*1*10^12;
119     refractive_index(:,N) = c./(d.*omega).*match_phase(:,N)+1;
120     extinction(:,N) = (c./(d*omega)').*log(transmission_absolute(:,N)');
121     absorption_coefficient(:,N) = -(2/d)*log(transmission_absolute(:,N)');
122     absorption(:,N) = absorption_coefficient(:,N)/100;
123
124
125     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
126     %   Refractive index, extinction and absorption coefficient analysis   %
127     %   for reference and sample (polymer measurement).                 %
128     %                                                                 %
129     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
130
131     % omega = 2*pi*frequency*1*10^12;
132     % refractive_index(:,N) = 1+(c*match_phase(:,N)./(d*omega));
133     % absorption_coefficient(:,N) = -(2/d)*log((1+refractive_index(:,N)).*
134     % (1+refractive_index(:,N)).*transmission_absolute(:,N)./
135     % (4.*refractive_index(:,N))));
136     % absorption(:,N) = absorption_coefficient(:,N)/100;
137
138     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
139     % Double Debye relaxation model for liquid measurement. The fitting   %
140     % parameters are obtained from J. T. Kindt et. al (1996).           %
141     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
142
143     %Double Debye model for water
144     test = 3.48 + (78.36-4.93)./(1-8.24*10^(-12)*omega*i) + (4.93-3.48)./
```

```

145     (1-0.182*10(-12)*omega*i);
146
147     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
148     % Triple Debye relaxation model for liquid measurement. The fitting %
149     % parameters are ontained from J. T. Kindt et. al (1996).          %
150     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
151
152     %Double Debye model for ethanol
153     % test  = 1.93 + (24.35-4.15)./(1+161*10(-12)*omega*i) + (4.15-2.72)./
154     % (1+3.3*10(-12)*omega*i)+(2.72-1.93)./(1+0.22*10(-12)*omega*i);
155
156     %Double Debye model for methanol
157     %test  = 2.10 + (32.63-5.35)./(1+48*10(-12)*omega*i) + (5.35-3.37)./
158     % (1+1.25*10(-12)*omega*i)+(3.37-2.10)./(1+0.16*10(-12)*omega*i);
159
160     test_real = real(test);
161     test_imag = imag(test);
162     test_index = sqrt(((sqrt((test_real.*test_real)+(test_imag.*test_imag)))
163     + test_real)*0.5);
164
165     test_alphax =2.*omega./c;
166     test_alpha = (test_alphax.*sqrt(((sqrt((test_real.*test_real)
167     + (test_imag.*test_imag))) - test_real)*0.5))/100;
168
169     % Plot the terahertz reference and sample pulses in time domain.
170     graph_one = figure(1);
171     subplot(2,1,1);
172     plot(sammatrix_time(:,N),smatrix_amp(:,N),'b','linewidth',1);
173     hold on
174     plot(refmatrix_time(:,N),rmatrix_amp(:,N),'b','linewidth',1);
175     grid on
176
177     % Plot the spectral amplitude in frequency domain.
178     subplot(2,1,2);
179     semilogy(frequency(1:m/2),reference_absolute(1:m/2,N),'b','linewidth',1);
180     hold on
181     semilogy(frequency(1:m/2),sample_absolute(1:m/2,N),'b','linewidth',1);
182     grid on
183
184     % Plot the original and extrapolated phases in frequency domain.
185     graph_two = figure(2);
186     subplot(2,1,1);

```


D.2 Double-modulated THz-DTDS analysis program

```
187     plot(frequency(1:m/2),normal_phase(1:m/2,N),'b','linewidth',1);
188     hold on
189     plot(frequency(1:m/2),match_phase(1:m/2,N),'g','linewidth',1);
190     grid on
191
192     % Plot the transmission coefficient in frequency domain.
193     transmission_absolute(:,N) = transmission_absolute(:,N)*100;
194
195     subplot(2,1,2);
196     plot(frequency(1:m/2),transmission_absolute(1:m/2,N),'b','linewidth',1);
197     grid on
198
199     % Comparison of refractive index obtained from the measurement with the
200     % refractive index obtained from the Debye relaxation model.
201
202     graph_three = figure(3);
203     subplot(2,1,1);
204     plot(frequency(1:m/2),refractive_index(1:m/2,N),'b','linewidth',1);
205     hold on
206     plot(frequency(1:m-2),test_index(1:m-2),'b','linewidth',2);
207     grid on
208
209     % Comparison of absorption coefficient obtained from the measurement with
210     % the absorption coefficient obtained from the Debye relaxation model.
211     subplot(2,1,2);
212     plot(frequency(1:m/2),absorption(1:m/2,N),'b','linewidth',1);
213     hold on
214     plot(frequency(1:m-2),test_alpha(1:m-2),'b','linewidth',2);
215     grid on
216
217 end
218
219 mean_smatrix_amp = mean(smatrix_amp,2);
220 mean_samatrix_time = mean(samatrix_time,2);
221 mean_rmatrix_amp = mean(rmatrix_amp,2);
222 mean_refmatrix_time = mean(refmatrix_time,2);
223 mean_sample_absolute = mean(sample_absolute,2);
224 mean_reference_absolute = mean(reference_absolute,2);
225 mean_normal_phase = mean(normal_phase,2);
226 mean_match_phase = mean(match_phase,2);
227 mean_transmission_absolute = mean(transmission_absolute,2);
228 mean_refractive_index = mean(refractive_index,2);
```

```
229 mean_absorption = mean(absorption,2);
230
231 % Calculating standard deviation for the refractive index
232 standard_dev_refrac = std(refractive_index,0,2);
233
234 % Calculating standard deviation for the absorption coeff
235 standard_dev_absorp = std(absorption,0,2);
236
237
238 % Plot the averaged terahertz reference and sample pulses in time domain.
239 graph_one = figure(1);
240     subplot(2,1,1);plot(mean_refmatrix_time(1:m/2),mean_rmatrix_amp(1:m/2)
241         , 'r', 'linewidth', 2);
242     hold on
243     plot(mean_refmatrix_time(1:m/2),mean_smatrix_amp(1:m/2), 'g', 'linewidth'
244         , 2);
245     grid on
246     legend('Reference', 'Sample', 1);
247     title('Temporal pulse shape of xxx');
248     xlabel('Time (ps)');
249     ylabel('Amplitude (a.u)');
250
251 % Plot the averaged spectral amplitude in frequency domain.
252     subplot(2,1,2);
253     semilogy(frequency(1:m/2),mean_reference_absolute(1:m/2), 'r', 'linewidth', 2);
254     hold on
255     semilogy(frequency(1:m/2),mean_sample_absolute(1:m/2), 'g', 'linewidth', 2);
256     grid on
257     legend('Reference', 'Sample', 1);
258     title('Spectral amplitude of xxx');
259     xlabel('Frequency (THz)');
260     ylabel('Spectral amplitude (a.u)');
261
262 % Plot the averaged original and extrapolated phases in frequency domain.
263 graph_two = figure(2);
264     subplot(2,1,1);
265     plot(frequency(1:m/2),mean_normal_phase(1:m/2), 'b', 'linewidth', 2);
266     hold on
267     plot(frequency(1:m/2),mean_match_phase(1:m/2), 'c', 'linewidth', 2);
268     grid on
269     legend('Original', 'Extrapolated', 1);
270     title('Phase of xxx');
```

D.2 Double-modulated THz-DTDS analysis program

```
271     xlabel('Frequency (THz)');
272     ylabel('Phase (rad)');
273
274 % Plot the averaged transmission coefficient in frequency domain.
275     subplot(2,1,2);
276     plot(frequency(1:m/2),mean_transmission_absolute(1:m/2),'r','linewidth',1);
277     grid on
278     title('Transmission coefficient of xxx');
279     xlabel('Frequency (THz)');
280     ylabel('Transmission (%)');
281
282 % Plot the averaged, smoothed, and errorbar of the refractive index in
283 % frequency domain.
284 graph_three = figure(3);
285     subplot(2,1,1);
286     plot(frequency(1:m/2),mean_refractive_index(1:m/2),'r','linewidth',2);
287     hold on
288     for s = 1:(m-2)
289         average_REF(s) = mean((mean_refractive_index(s)+mean_refractive_index
290             (s+1))/2);
291     end
292     errorbar(frequency(1:10:m/6),mean_refractive_index(1:10:m/6),
293         standard_dev_refrac(1:10:m/6),'k','linewidth',1.5);
294     hold on
295     plot(frequency(1:m-2),average_REF(1:m-2),'g','linewidth',2);
296     grid on
297     title('Refractive index of xxx ');
298     legend('Original','Smoothed',1)
299     xlabel('Frequency (THz)');
300     ylabel('Refractive index (n)');
301
302 % Plot the averaged, smoothed, and errorbar of the absorption coefficient in
303 % frequency domain.
304     subplot(2,1,2);
305     plot(frequency(1:m/2),mean_absorption(1:m/2),'r','linewidth',1);
306     hold on
307     for s = 1:(m-2)
308         average_abs(s) = mean((mean_absorption(s)+mean_absorption(s+1))/2);
309     end
310     errorbar(frequency(1:14:m/6),mean_absorption(1:14:m/6),
311         standard_dev_absorp(1:14:m/6),'k','linewidth',2);
312     hold on
```

```

313     plot(frequency(1:m-2),average_abs(1:m-2),'g','linewidth',2);
314     grid on
315     title('Absorption coefficient of xxx')
316     legend('Original','Smoothed',1)
317     xlabel('Frequency (THz)');
318     ylabel('Absorption coefficient (\alpha)');
319
320     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
321     %                               End of the program                               %
322     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

D.3 Modelling conventional THz-TDS signal extraction

```

1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %   Simulation program to model terahertz signal extraction from a           %
3  %   conventional THz-TDS spectrometer.                                     %
4  %                                                                                   %
5  % Jegathisvaran Balakrishnan                                               %
6  % The University of Adelaide                                               %
7  % December 2009                                                            %
8  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
9
10 clear all;
11 % Load original signal for simulation
12 fid1 = fopen('Simulation\xxxx','r');
13 reference_scan1 = textscan(fid1,'%f %f','headerlines',2);
14 reference_amplitudel = reference_scan1{: ,2};
15 reference_timel = reference_scan1{: ,1};
16 fclose(fid1);
17
18 [m,n] = size(reference_amplitudel(:,1));
19 timestep = mean(diff(reference_timel(1:m)))./10;
20
21 fs = 10000; % Sampling frequency
22 fc = 0.35; % cutoff frequency
23 Δ = timestep;
24 num_sam = m;
25 time = (0:num_sam-1)*Δ; %time axis
26 frequency = [0:num_sam-1]'/Δ/num_sam;
27 chopperfreq = 2.0;% chopper frequency in Hz
28 fchopper = sin(2*pi*chopperfreq*time);
29

```

D.3 Modelling conventional THz-TDS signal extraction

```
30 nth = 6;% filter order
31 %harmonics generation using for loop is require to create square wave out
32 %of sine wave
33 for k = 2:3
34     fchopper = fchopper + sin(((2*k)-1).*2*pi*chopperfreq*time)/((2*k)-1);
35 end
36 fchopper = (fchopper*4)/pi;
37
38 % nth order low pass Butterworth filter
39 [B A] = butter(nth,fc/(fs/80));
40 h = freqs(B,A,frequency);
41 mag = 20*log10(abs(h));
42 figure(1);
43 semilogx(frequency,mag)
44 xlabel('Frequency in Hz');
45 ylabel('Magnitude (dB)');
46
47 detector=[];
48 lock_in_t=[];
49 lock_in_nt=[];
50 lock_in_fft_nt=[];
51 butter_gaussian=[];
52 butter_gaussian_fft=[];
53 inverse_origin_fft=[];
54 inverse_gaussian_fft=[];
55
56 % modulated raw output without noise
57 for s = 1:length(reference.amplitudel)
58     for s1 = 1:length(fchopper)
59         detector(s,s1) = (fchopper(s1).*reference.amplitudel(s));
60     end
61 end
62
63 % demodulated output without noise
64 for s = 1:length(reference.amplitudel)
65     for s1 = 1:length(fchopper)
66         lock_in_t(s,s1) = (detector(s,s1)*fchopper(s1));
67     end
68 end
69
70 % Add white noise to the modulated signal
71 for s = 1:length(reference.amplitudel)
```

```
72     testDt = [];  
73     testDt = awgn(detector(s,:),10,'measured');  
74     for s1 = 1:length(fchopper)  
75         detector.nt(s,s1) = testDt(s1);  
76     end  
77 end  
78  
79 % Add white noise to the demodulated signal  
80 for s = 1:length(reference_amplitudel)  
81     testD = [];  
82     testD = awgn(lock_in_t(s,:),10,'measured');  
83     for s1 = 1:length(fchopper)  
84         lock_in.nt(s,s1) = testD(s1);  
85     end  
86 end  
87  
88 % FFT the noise added modulated signal  
89 for s = 1:length(reference_amplitudel)  
90     signoisedt = [];  
91     signoisedt = fft(detector.nt(s,:));  
92     for s1 = 1:length(fchopper)  
93         detector.fft.nt(s,s1) = signoisedt(s1);  
94     end  
95 end  
96  
97 % FFT the noise added demodulated signal  
98 for s = 1:length(reference_amplitudel)  
99     signoise = [];  
100    signoise = fft(lock_in.nt(s,:));  
101    for s1 = 1:length(fchopper)  
102        lock_in.fft.nt(s,s1) = signoise(s1);  
103    end  
104 end  
105  
106 % Apply butterworth nth order filter to introduce 1/f noise  
107 for s = 1:length(reference_amplitudel)  
108     testE = [];  
109     testE = filter(B,A,lock_in.nt(s,:));  
110     for s1 = 1:length(fchopper)  
111         butter_gaussian(s,s1) = testE(s1);  
112     end  
113 end
```

D.3 Modelling conventional THz-TDS signal extraction

```
114
115 % FFT the butterworth nth order filter
116 for s = 1:length(reference.amplitudel)
117     testF = [];
118     testF = fft(butter_gaussian(s,:));
119     for s1 = 1:length(fchopper)
120         butter_gaussian_fft(s,s1) = testF(s1);
121     end
122 end
123
124
125
126 % Inverse FFT of the filter for recovering the original signal after filtering
127 for s = 1:length(reference.amplitudel)
128     testG = [];
129     testG = ifft(butter_gaussian_fft(s,:));
130     for s1 = 1:length(fchopper)
131         inverse_gaussian_fft(s,s1) = testG(s1);
132     end
133 end
134
135 % Recovering the averaged original input signal after filtering
136 y=[];
137 for s = 1:length(reference.amplitudel)
138     y(s) = mean(inverse_gaussian_fft(s,:));
139 end
140
141 % Plot the modulated, demodulated, butterworth low-pass filtered signals in
142 % time domain
143 pause
144 graph2 = figure(2);
145 subplot(2,1,1);plot(time,detector(150,:), 'r');
146 hold on
147 plot(time,lock_in_nt(150,:), 'b');
148 hold on
149 plot(time,butter_gaussian(150,:), 'g');
150 legend('Modulated signal','Demodulated signal','Butterworth LPF');
151 xlabel('Time in sec');
152 ylabel('Amplitude (a.u)');
153 title('Before and after butterworth low-pass filter at 150th step of the
154 delay stage');
155
```

```

156 % Plot the modulated, demodulated, butterworth low-pass filtered signals in
157 % frequency domain
158
159 subplot(2,1,2);plot(frequency,abs(detector_fft_nt(150,:)), 'r');
160 hold on
161 plot(frequency,abs(lock_in_fft_nt(150,:)), 'b');
162 hold on
163 plot(frequency,abs(butter_gaussian_fft(150,:)), 'g');
164 legend('Modulated signal', 'Demodulated signal', 'Butterworth LPF');
165 xlabel('Frequency in Hz');
166 ylabel('Amplitude (a.u)');
167 title('Before and after butterworth low-pass filter at 150th step of the
168 delay stage');
169
170 % Plot the original signal and compare it the signal recovered after
171 % filtering process
172 pause
173 graph3 = figure(3);
174 plot(time,reference_amplitudel, 'b')
175 hold on
176 plot(time,y, 'r');
177 xlabel('Time in sec');
178 ylabel('Amplitude (a.u)');
179 title('Original signal', 'Recovered terahertz signal');

```

D.4 Modelling double-modulated THz-DTDS signal extraction

```

1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %           Simulation program to model terahertz signal extraction      %
3 %           from a double-modulated terahertz double-modulated         %
4 %           differential time-domain spectroscopy.                       %
5 %                                                                           %
6 % Jegathisvaran Balakrishnan                                           %
7 % The University Adelaide                                               %
8 % December 2009                                                         %
9 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
10
11 clear all;
12 % Load mean signal for simulation
13 fid1 = fopen('Simulation\Mean.dat', 'r');

```


D.4 Modelling double-modulated THz-DTDS signal extraction

```
14 reference_scan1 = textscan(fid1,'%f %f','headerlines',2);
15 reference_amplitudel = reference_scan1{: ,2};
16 reference_time1 = reference_scan1{: ,1};
17 fclose(fid1);
18
19 % Load amplitude signal for simulation
20 fid2 = fopen('Simulation\Amplitude.dat','r');
21 reference_scan2 = textscan(fid2,'%f %f','headerlines',2);
22 reference_amplitude2 = reference_scan2{: ,2};
23 reference_time2 = reference_scan2{: ,1};
24 fclose(fid2);
25
26 [m,n] = size(reference_amplitudel(:,1));
27 timestep = mean(diff(reference_time1(1:m)))./10;
28
29 fs = 100000; % sampling frequency
30 fc = 0.8; % cutoff frequency
31 Δ = timestep;
32 num_sam = m;
33 time = (0:num_sam-1)*Δ; %time axis
34 frequency = [0:num_sam-1]'/Δ/num_sam;
35 chopperfreq = 3.0;% chopper frequency in Hz
36 fchopper = sin(2*pi*chopperfreq*time);
37 wheelfreq = 0.5;% wheel frequency in Hz
38 fwheel = sin(2*pi*rotatorfreq*time);
39 nth = 1;% filter order
40
41 % harmonics generation using for loop is require to create square wave out
42 % of sine wave
43 for k = 2:2
44     fchopper = fchopper + sin((2*k-1).*2*pi*chopperfreq*time)/((2*k)-1);
45     fwheel = fwheel + sin((2*k-1).*2*pi*wheelfreq*time)/((2*k)-1);
46 end
47 fchopper = (fchopper*4)/pi+1;
48 fwheel = (fwheel*4)/pi+1;
49
50 % Equation 10.9 in Ch. 10. Simulated double-modulated terahertz signal
51 % at the detector
52 Amp=max(fwheel); % Reference thickness
53 xTh=0.2; % Sample thickness
54 fwheel2=[]; fcpct=1;
55 for fchct=1:length(fwheel)
```

```

56     fwheel2(fcpct) = (((Amp-xTh)/Amp)*fwheel(fchct))+xTh;
57     fcpct=fcpct+1;
58 end
59 fmod = fchopper.*frotator2;
60
61 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
62
63 % nth order low pass Butterworth filter
64 [B A] = butter(nth,fc/(fs/80));
65 h = freqs(B,A,frequency);
66 mag = 20*log10(abs(h));
67 figure(1);
68 semilogx(frequency,mag)
69 xlabel('Frequency in Hz');
70 ylabel('Magnitude (dB)');
71
72
73 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
74 %           Recovering mean signal without introducing any noise           %
75 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
76 detector=[];
77 detector_fft_t=[];
78 lock_in_t=[];
79 lock_in_fft_t=[];
80 lock_in_fft_nt=[];
81 butter_origin=[];
82 butter_origin_fft=[];
83 butter_gaussian=[];
84 butter_gaussian_fft=[];
85 inverse_origin_fft=[];
86 inverse_gaussian_fft=[];
87 lock_in_nt=[];
88
89 % Double-modulated raw output without noise
90 for s = 1:length(reference_amplitude1)
91     for s1 = 1:length(fchopper)
92         detector(s,s1) = fmod(s1).*reference_amplitude1(s);
93     end
94 end
95
96 % FFT of the double-modulated raw output without noise
97 for s = 1:length(reference_amplitude1)

```

D.4 Modelling double-modulated THz-DTDS signal extraction

```
98     sigdt = [];  
99     sigdt = fft(detector(s,:));  
100    for s1 = 1:length(fchopper)  
101        detector_fft_t(s,s1) = sigdt(s1);  
102    end  
103 end  
104  
105 % Demodulated signal without any filtering and noise (mixer output, LIA1  
106 % PSD output)  
107 for s = 1:length(reference.amplitudel)  
108     for s1 = 1:length(fchopper)  
109         lock_in_t(s,s1) = detector(s,s1)*fchopper(s1);  
110     end  
111 end  
112  
113 % FFT Demodulated signal without any filtering and noise (mixer output,  
114 % LIA1 PSD output)  
115 for s = 1:length(reference.amplitudel)  
116     sigX = [];  
117     sigX = fft(lock_in_t(s,:));  
118     for s1 = 1:length(fchopper)  
119         lock_in_fft_t(s,s1) = sigX(s1);  
120     end  
121 end  
122  
123 % Apply butterworth nth order filter to extract mean signal  
124 for s = 1:length(reference.amplitudel)  
125     testA = [];  
126     testA = filter(B,A,lock_in_t(s,:));  
127     for s1 = 1:length(fchopper)  
128         butter_origin(s,s1) = testA(s1);  
129     end  
130 end  
131  
132 % FFT the butterworth nth order filter  
133 for s = 1:length(reference.amplitudel)  
134     testB = [];  
135     testB = fft(butter_origin(s,:));  
136     for s1 = 1:length(fchopper)  
137         butter_origin_fft(s,s1) = testB(s1);  
138     end  
139 end
```

```

140
141 % Inverse FFT of the filter for recovering the original mean signal after
142 % filtering
143 for s = 1:length(reference_amplitude1)
144     testC = [];
145     testC = ifft(butter_origin_fft(s,:));
146     for s1 = 1:length(fchopper)
147         inverse_origin_fft(s,s1) = testC(s1);
148     end
149 end
150
151 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
152 %           Recovering amplitude signal without introducing any noise           %
153 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
154
155 % Demodulate the mixer output with fwheel(spining wheel)
156 for s = 1:length(reference_amplitude1)
157     for s1 = 1:length(fchopper)
158         lock_2in_t(s,s1) = (lock_in_t(s,s1)*fwheel(s1));
159     end
160 end
161
162 % FFT of the demodulated output signal
163 for s = 1:length(reference_amplitude1)
164     sig = [];
165     sig = fft(lock_2in_t(s,:));
166     for s1 = 1:length(fchopper)
167         lock_2in_fft_t(s,s1) = sig(s1);
168     end
169 end
170
171 % Apply butterworth nth order filter to extract amplitude signal
172 for s = 1:length(reference_amplitude1)
173     testAx = [];
174     testAx = filter(B,A,lock_2in_t(s,:));
175     for s1 = 1:length(fchopper)
176         butter_2origin(s,s1) = testAx(s1);
177     end
178 end
179
180 % FFT the butterworth nth order filter
181 for s = 1:length(reference_amplitude1)

```

D.4 Modelling double-modulated THz-DTDS signal extraction

```
182     testBx = [];  
183     testBx = fft(butter_2origin(s,:));  
184     for s1 = 1:length(fchopper)  
185         butter_2origin_fft(s,s1) = testBx(s1);  
186     end  
187 end  
188  
189 % Inverse FFT of the filter for recovering the original amplitude signal after  
190 % filtering  
191 for s = 1:length(reference_amplitudel)  
192     testCx = [];  
193     testCx = ifft(butter_2origin_fft(s,:));  
194     for s1 = 1:length(fchopper)  
195         inverse_2origin_fft(s,s1) = testCx(s1);  
196     end  
197 end  
198  
199 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%  
200 %             Recovering mean signal with Gaussian noise             %  
201 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%  
202  
203 % Adding gaussian noise on the double-modulated signal  
204 for s = 1:length(reference_amplitudel)  
205     testDt = [];  
206     testDt = awgn(detector(s,:),10,'measured');  
207     for s1 = 1:length(fchopper)  
208         detector_nt(s,s1) = testDt(s1);  
209     end  
210 end  
211  
212 % FFT the double-modulated signal with noise Gaussian noise  
213 for s = 1:length(reference_amplitudel)  
214     signoisedt = [];  
215     signoisedt = fft(detector_nt(s,:));  
216     for s1 = 1:length(fchopper)  
217         detector_fft_nt(s,s1) = signoisedt(s1);  
218     end  
219 end  
220  
221 % Adding gaussian noise to the demodulated signal  
222 for s = 1:length(reference_amplitudel)  
223     testD = [];
```

```
224     testD = awgn(lock_in_t(s,:),10,'measured');
225     for s1 = 1:length(fchopper)
226         lock_in_nt(s,s1) = testD(s1);
227     end
228 end
229
230 % FFT the demodulated signal
231 for s = 1:length(reference.amplitude1)
232     signoise = [];
233     signoise = fft(lock_in_nt(s,:));
234     for s1 = 1:length(fchopper)
235         lock_in_fft_nt(s,s1) = signoise(s1);
236     end
237 end
238
239 % Apply butterworth nth order filter to extract mean signal
240 for s = 1:length(reference.amplitude1)
241     testE = [];
242     testE = filter(B,A,lock_in_nt(s,:));
243     for s1 = 1:length(fchopper)
244         butter_gaussian(s,s1) = testE(s1);
245     end
246 end
247
248 % FFT the butterworth filtered mean signal
249 for s = 1:length(reference.amplitude1)
250     testF = [];
251     testF = fft(butter_gaussian(s,:));
252     for s1 = 1:length(fchopper)
253         butter_gaussian_fft(s,s1) = testF(s1);
254     end
255 end
256
257 % Inverse FFT to recover the original mean signal
258 for s = 1:length(reference.amplitude1)
259     testG = [];
260     testG = ifft(butter_gaussian_fft(s,:));
261     for s1 = 1:length(fchopper)
262         inverse_gaussian_fft(s,s1) = testG(s1);
263     end
264 end
265
```

D.4 Modelling double-modulated THz-DTDS signal extraction

```
266 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
267 %           Recovering amplitude signal with Gaussian noise           %
268 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
269
270 % Adding gaussian noise to the demodulated signal of lock-in amplifier two
271 % (PSD output of lock-in amplifier two)
272 for s = 1:length(reference.amplitudel)
273     testDx = [];
274     testDx = awgn(lock_2in_t(s,:),10,'measured');
275     for s1 = 1:length(fchopper)
276         lock_2in_nt(s,s1) = testDx(s1);
277     end
278 end
279
280 % FFT the PSD output of lock-in amplifier two
281 for s = 1:length(reference.amplitudel)
282     signoiseX = [];
283     signoiseX = fft(lock_2in_nt(s,:));
284     for s1 = 1:length(fchopper)
285         lock_2in_fft_nt(s,s1) = signoiseX(s1);
286     end
287 end
288
289 % Introducing butterworth filtering to the PSD out signal
290 for s = 1:length(reference.amplitudel)
291     testEx = [];
292     testEx = filter(B,A,lock_2in_nt(s,:));
293     for s1 = 1:length(fchopper)
294         butter_2gaussian(s,s1) = testEx(s1);
295     end
296 end
297
298 % FFT of the filtered signal
299 for s = 1:length(reference.amplitudel)
300     testFx = [];
301     testFx = fft(butter_2gaussian(s,:));
302     for s1 = 1:length(fchopper)
303         butter_2gaussian_fft(s,s1) = testFx(s1);
304     end
305 end
306
307 % Inverse FFT of the filtered signal to recover the original input
```

```

308 % amplitude signal
309 for s = 1:length(reference.amplitude1)
310     testGx = [];
311     testGx = ifft(butter_2gaussian_fft(s,:));
312     for s1 = 1:length(fchopper)
313         inverse_2gaussian_fft(s,s1) = testGx(s1);
314     end
315 end
316
317 % Averaging the inverse FFT of the filtered mean signal
318 y=[];
319 for s = 1:length(reference.amplitude1)
320     y(s) = mean(inverse_gaussian_fft(s,:));
321 end
322
323 % Averaging the inverse FFT of the filtered amplitude signal
324 h=[];
325 for s = 1:length(reference.amplitude1)
326     h(s) = mean(inverse_2gaussian_fft(s,:));
327 end
328
329 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
330 %               Plot signals in time and frequency domains           %
331 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
332 pause
333 graph2 = figure(2);
334
335 % Plot the fchopper signal and fwheel2 signal in time domain
336 subplot(2,1,1);
337 plot(time,fchopper,'g');
338 hold on
339 plot(time,fwheel2,'b');
340 legend('Chopper frequency','Spinning wheel frequency');
341 xlabel('Time in sec');
342 ylabel('Amplitude (a.u)');
343 title('Reference signals');
344
345 % Plot the modulated, demodulated, butterworth low-pass filtered signals in
346 % time domain
347 subplot(2,1,2);
348 plot(time,detector(350,:), 'c');
349 hold on

```


D.4 Modelling double-modulated THz-DTDS signal extraction

```
350 plot(time,lock_in_t(350,:), 'b');
351 hold on
352 plot(time,lock_2in_t(350,:), 'r');
353 hold on
354 plot(time,lock_in_nt(350,:), 'g');
355 hold on
356 plot(time,lock_2in_nt(350,:), 'k');
357 legend('Modulated signal at 350th step', 'LIA1 PSD output at 350th step',
358 'LIA2 PSD output at 350th step', 'LIA1 PSD output at 350th step (with noise)',
359 'Amplitude+noise at 350th step (with noise)', 1);
360 xlabel('Time in sec');
361 ylabel('Amplitude (a.u)');
362 title('Signal detected at the 350th step of the delay stage (with and without
363 gaussian noise)');
364
365 % Plot the modulated, demodulated, butterworth low-pass filtered signals in
366 % frequency domain (without Gaussian noise)
367 graph3 = figure(3);
368
369 subplot(2,1,1);
370 plot(frequency,abs(detector_fft_t(350,:)), 'c');
371 hold on
372 pause;
373 plot(frequency,abs(lock_in_fft_t(350,:)), 'b');
374 hold on
375 pause;
376 plot(frequency,abs(lock_2in_fft_t(350,:)), 'r');
377 hold on
378 pause;
379 plot(frequency,abs(butter_origin_fft(350,:)), 'g');
380 hold on
381 pause;
382 plot(frequency,abs(butter_2origin_fft(350,:)), 'k');
383 legend('Modulated signal at 350th step', 'Demodulated output (LIA1) at 350th step ',
384 'Demodulated output (LIA2) at 350th step',
385 'Demodulated output after LPF (LIA1) at 350th step',
386 'Demodulated output after LPF (LIA2) at 350th step', 1);
387 xlabel('Frequency in Hz');
388 ylabel('Amplitude (a.u)');
389 title('Before and after butterworth low-pass filter at 350th step of the
390 delay stage');
391
```

```
392 % Plot the modulated, demodulated, butterworth low-pass filtered signals in
393 % frequency domain (with Gaussian noise)
394 subplot(2,1,2)
395 plot(frequency,abs(detector_fft_nt(350,:)), 'c');
396 pause;
397 hold on
398 plot(frequency,abs(lock_in_fft_nt(350,:)), 'b');
399 pause;
400 hold on
401 plot(frequency,abs(lock_2in_fft_nt(350,:)), 'r');
402 pause
403 hold on
404 plot(frequency,abs(butter_gaussian_fft(350,:)), 'g');
405 pause
406 hold on
407 plot(frequency,abs(butter_2gaussian_fft(350,:)), 'k');
408 legend('Modulated signal at 350th step', 'Demodulated output (LIA1) at 350th step',
409 'Demodulated output (LIA2) at 350th step',
410 'Demodulated output after LPF (LIA1) at 350th step',
411 'Demodulated output after LPF (LIA2) at 350th step',1);
412 xlabel('Frequency in Hz');
413 ylabel('Amplitude (a.u)');
414 title('Before and after butterworth low-pass filter at 350th step of the
415 delay stage with gaussian noise');
416 pause
417
418 % Plot the original mean and amplitude signals and compare it the signals
419 % recovered after filtering process
420 graph4 = figure(4);
421 plot(time,reference_amplitude1, 'b')
422 hold on
423 plot(time,reference_amplitude2, 'k')
424 hold on
425 plot(time,y, 'r');
426 hold on
427 plot(time,h, 'g');
428 legend('Original mean', 'Original amplitude', 'Recovered mean', 'Recovered
429 amplitude');
430 xlabel('Time in sec');
431 ylabel('Amplitude (a.u)');
```


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Symbols & Glossary

The commonly used acronyms and symbols used in this Thesis is given in the table below. The page numbers for each entry refer to the first use of the symbol or acronym in the text.

Symbols & Acronyms	Description	Page
H	magnetic field	8
E	electric field	8
<i>f</i>	frequency (Hertz)	8
<i>E</i>	photon energy	8
<i>h</i>	Planck's constant (Joules per second)	8
λ	wavelength (m)	8
ASTM D570	standard test method for water absorption of plastics 1986	63
BNC	bayonet neill-concelman	33
COC	cyclic-olefin copolymer	51
CPM	colliding-pulse passively modelocked	22
CFC	chlorofluorocarbon	50
CS ₂	carbon disulphide	72
DNA	deoxyribonucleic acid	73
ESR	electron spin resonance	9
EO	electro-optic	22
FTIR	Fourier transform infrared	48
FTIR-ATR	Fourier transform infrared - attenuated total reflectance	63
GaAs	gallium arsenide	2
GPIB	general purpose interface bus	158
HDPE	high density polyethylene	5
IR	infrared	13
LIA1	lock-in amplifier one	95
LIA2	lock-in amplifier two	96
LPF	low pass filter	155

Symbols & Acronyms	Description	Page
MW	megawatt	10
MD	molecular dynamics	73
Mb	myoglobin	73
MRI	magnetic resonance imaging	90
NMR	nuclear magnetic resonance	9
ND	neutral density	157
PMMA	poly(methyl methacrylate)	5
PVC	polyvinyl chloride	5
PTFE	polytetrafluoroethylene	5
PC	polycarbonate	58
PCB	printed circuit board	33
PE	polyethylene	73
PET	polyethylene terephthalate	73
PSD	phase sensitive detection	126
SOS	silicon-on-sapphire	2
SC	Subtilisin Carlsberg	73
SNR	signal-to-noise ratio	90
THz	terahertz	2
THz-TDS	terahertz time-domain spectroscopy	4
THz-DTDS	terahertz differential time-domain spectroscopy	4
TCF	analytic time correlation function	73
TIR	total internal reflection	87
TD-ATR	time-domain attenuated total reflection	110
UV	ultraviolet	15

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- α -ray, 17
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- γ -ray, 3, 7, 9, 16, 17, 19

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Résumé

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Scientific Genealogy

Scientific Genealogy of Jegathisvaran Balakrishnan

